Observed and Simulated Damage to Wooden Houses in Japan due to Recent Earthquakes

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H. Kawakami Geosphere Research Institute, Saitama University, Japan

SUMMARY:

The Kobe earthquake in 1995 caused tremendous loss of lives resulting from the collapse and damage of such structures that significantly affected economic condition. This disaster motivated many researchers to study the mechanisms of collapse of engineering structures in order to prevent further loss of lives in the future. In this paper, an innovative methodology in simulating the dynamic response of wood-framed buildings, for purposes of seismic performance assessment and retrofitting, is presented. The proposed method, which can simulate inelastic behavior of structures, is capable of showing realistic progressive collapse mechanisms and accurate seismic response of structures. The sequence of analyses and results in the form of computer animations are used to help building owners gain a better understanding of the seismic performance of their buildings before and after the structural reinforcement. Applications to real wood-framed residential buildings were used to show the effectiveness of the methodology in seismic performance assessment as well as retrofit plan development.

Keywords: Wooden houses, collapse, retrofitting, rigid body-spring method, simulation

1. INTRODUCTION

The evolution in computer hardware has significant impact on computing science and engineering design. In civil engineering, computer experiments utilizing multimedia and realistic computer animation reinforce, if not replace, traditional expensive experiments. Computer experiments offer several advantages such that they allow analysis of structures at full-scale, experiments may be performed at ideal conditions when necessary e.g. no air resistance or friction, and they are not subject to physical limitations inherent to experimental set-ups, e.g. maximum displacement/velocity of shaking tables, etc.

Efforts to simulate response of built structures to strong motion earthquakes attracted many researchers in the field of architecture and civil engineering. One of the most familiar accelerogram used is that of the Kobe earthquake in Japan which occurred in January 17, 1995 and caused enormous damage and destruction of structures and deaths in Kobe and in nearby areas. The disaster claimed more than 6,000 deaths, injured more than 35,000 people and caused about 10 trillion yen worth of damage. The death toll was reported to be mostly caused by collapse of buildings and breakdown of other civil engineering facilities. Investigation further revealed that most deaths were due to collapse of traditional wooden houses. This fact motivated structural and earthquake engineers to study the mechanisms of collapse of each wooden house and building in order to guarantee the safety of the general public in the occurrence of future earthquakes.

Analysis of the collapse of engineering structures subjected to strong ground motions or even blast loads, may be performed using a handful of methods. The popular finite element method allows modeling of structures at the material level, but its computational complexity has restricted its application to analysis of basic structural elements such as beams, columns, and joints. Finite element analysis of an entire structure was regarded to be too tedious and that dynamic analysis exhibiting strong nonlinearity and discontinuity requires a lot of computer power.

This study presents a three-dimensional simulation of structure collapse during strong motion earthquakes, such as the 1995 Kobe earthquake, using Rigid Body-Spring Method (RBSM). Various modes of collapse of a wooden structure modeled as an assembly of rigid bodies connected by inelastic links at their ends, will be presented. In modeling structural components, a link configuration is suggested to take into account structural damping and inelastic behavior.

The main objectives of this study are to understand the process in which wooden houses collapse during earthquakes and to identify and reinforce the weak point of the structure. Specifically, it aims to

- 1. simulate collapse mechanisms by modeling structural elements using rigid body-spring method implementing a configuration of inelastic links;
- 2. investigate how the collapse progresses from the local failures of the framing members; and
- 3. propose, with the use of an example, ways to reinforce a house to withstand strong ground shaking.

2. NONLINEAR ANALYSIS USING ASSEMBLY OF RIGID BODIES

Originally proposed by Kawai (1977), the basic approach of RBSM is to divide the given structure into appropriate number of rigid elements connected by spring systems. The displacements are completely described by the positions and rotations of the rigid bodies while the deformation energy of the structure is stored in the spring system.

In this paper, nonlinear analysis of structures will be carried out by introducing nonlinear springs to take into account large displacements and failure of structures during strong motion earthquakes.

2.1. Position and Orientation of Bodies

In rigid body assemblies, various coordinates systems must first be well understood (Fig. 1). A rigid body in space is positioned with respect to the inertial coordinate system OXYZ by a vector r attached to its mass center. Points that define the shape of the body or points where links are attached, say point a, are defined by a vector s in terms of local coordinates (with respect to Gxyz). If needed, the global coordinates of this point S are computed as

$$S = Rs + r \tag{2.1}$$

where R is a rotation matrix that transforms coordinates from Gxyz frame to OXYZ frame.

2.2. Governing Equations (Baraff 1992; Hamilton 1847)

To animate various systems using rigid bodies, appropriate forces must be taken into account. Forces that arise due to relative positioning of objects (e.g., contact or collision), object's velocity, connections (e.g., springs and dampers), and user-specified vector fields (e.g., gravity and other external forces) must be exerted on bodies properly. These forces induce linear and angular accelerations depending on the mass and mass distribution of the body, respectively.

The two fundamental equations used to analyze motions of rigid bodies in space are

$$\sum \boldsymbol{F}(t) = m \boldsymbol{\ddot{r}}(t) \tag{2.2}$$

$$\sum \boldsymbol{M}_{G}(t) = \dot{\boldsymbol{H}}_{G}(t) \tag{2.3}$$



Figure 1. Applied and effective forces on a rigid body and coordinate systems used in computer animation

where $\ddot{r}(t)$ is the acceleration of the center of mass and $\dot{H}_G(t)$ is the rate of change of the angular momentum about the mass center of the rigid body. If x, y and z axes coincide with the principal axes of inertia of the rigid body, Eqn. 2.3 can be expressed in terms of the inertia tensor I(t) as

$$\sum \boldsymbol{M}_{G}(t) = \boldsymbol{I}(t)\dot{\boldsymbol{\omega}}(t) \tag{2.4}$$

The above equations can be rewritten by first assuming

$$\dot{\boldsymbol{r}}(t) = \boldsymbol{v}(t) \tag{2.5}$$

$$\dot{\boldsymbol{q}}(t) = \frac{1}{2}\boldsymbol{\omega}(t) * \boldsymbol{q}(t) = \boldsymbol{g}(\boldsymbol{q}(t), \boldsymbol{\omega}(t))$$
(2.6)

where q(t) is Hamilton's quaternion, and $\omega(t) * q(t)$ denotes a shorthand of the multiplication of two quaternions $[0, \omega(t)]$ and q(t).

At any instant, the state of a rigid body is stored in a vector $\mathbf{x}(t)$ consisting of its position, orientation, and its linear and angular velocities (Baraff 1992). Mathematically collected as,

$$\boldsymbol{x}(t) = \begin{cases} \boldsymbol{r}(t) \\ \boldsymbol{q}(t) \\ \boldsymbol{v}(t) \\ \boldsymbol{\omega}(t) \\ \boldsymbol{\omega}(t) \end{cases}_{13\times 1}$$
(2.7)

The time derivative of the state vector can be set-up using Eqns. 2.3, 2.5, 2.6, and 2.7 as

$$\dot{\mathbf{x}}(t) = \begin{cases} \mathbf{v}(t) \\ \mathbf{g}(\mathbf{q}(t), \mathbf{\omega}(t)) \\ \sum_{I=1}^{I} \mathbf{F}(t) / m \\ \mathbf{I}^{-1}(t) \sum_{I} \mathbf{M}_{G}(t) \end{cases}$$
(2.8)

This system of first-order differential equations are sufficient to perform physically based animation of rigid bodies. Knowing the current state of the rigid bodies and the derivative information at any time, a differential equation solver can now be used to compute the state vector at a subsequent time. Euler

method, as given in Eqn. 2.9, for example can be used but since it is unstable and inaccurate, more sophisticated methods such as Runge-Kutta method are appropriate. Although they are more computationally expensive than Euler method, large step sizes can be used resulting in an overall computational savings.

$$\boldsymbol{x}(t+h) = \boldsymbol{x}(t) + h \cdot \dot{\boldsymbol{x}}(t) \tag{2.9}$$

Finally, it is important to note that the sum of forces and sum of moments about rigid body's mass center in Eqn. 2.8 include contact forces and collision forces (or impulses) when it moves relative to another rigid body. This of course entails the use of efficient collision detection routines. Since collision detection, response and contact handling are well documented in computer animation and robotics, it will not be discussed in detail in this paper.

3. EARTHQUAKE GROUND MOTIONS

Throughout the scope of this paper, the earthquake accelerogram used was that observed at Kobe Marine Meteorological Observatory during of the 1995 Kobe earthquake as shown in Fig. 2. The maximum accelerations in EW-, NS-, and UD-directions are 6.0 m/s² at 5.5 s, 8.2 m/s² at 5.5 s, and 3.3 m/s² at 4.7 s, respectively.



Figure 2. (a) Time history of ground acceleration of the 1995 Kobe earthquake used in analyses(b) Relationship between the scaling factor to multiply the time history shown in (a) and Japan Meteorological Agency seismic intensity scale

4. SYSTEM OF NON-LINEAR SPRINGS AND DASHPOTS

4.1. Deformations and Restoring Forces of a Link

A new link consisting of a spring and a damper, parallel to one another is introduced. Forces exerted to points on connected bodies are the vector sum of forces exerted by the spring and damper components.

The stress-strain behavior of materials, as modeled by springs, is idealized by the straight lines in Fig. 3. In this model the restoring force in tension is proportional to the strain up to ε_{YT} with maximum yield restoring force F_{YT} . The second straight line represents the strain-hardening characteristic until point C, when the restoring force reaches its ultimate value F_{UT} . For different set of parameters ε_{YC} , F_{YC} , ε_{UC} , and F_{UC} , the behavior in compression can be modeled.

The restoring force exerted by the damper can be computed similarly for any relative velocity as $v_{rel} = \mathbf{n} \cdot (\mathbf{v}_1 - \mathbf{v}_2)$.

If the strain in the link exceeds its maximum value ε_{UT} or ε_{UC} , no subsequent forces are exerted to the connected bodies. The link is marked DELETED to aid analysis of link failure.

4.2. Proposed System of Inelastic Links

To simulate inelastic behaviour of structural components, a configuration of nonlinear links are positioned.



Figure 3. Force exerted by a link on rigid bodies

5. APPLICATION TO WOODEN HOUSES

5.1. Dynamic Collapse of Conventional Wooden Houses

Using the numerical method presented above, earthquake responses of typical wooden houses in Japan were computed. In modeling, the dead load of the floor slab, beams, columns, walls and roofs, and the live loads were estimated. The stress-strain curves for the material of the structural members were modeled. The model structures were then subjected to doubly-amplified waves of the 1995 Kobe earthquake in Fig. 2, and various collapse mechanisms of wooden houses were observed including (a) collapse due to the soft first story, (b) tumbling type collapse, (c) failure at the second floor due to the amplification of the vibration at the upper floor, and (d) collapse of intermediate floor.



Figure 4. Progressive collapse sequence of a wooden house



Figure 5. Comparison between the response behaviors of the existing wooden house due to the earthquake ground motions (multiplication factors = 1, 1.5 and 2)



Figure 6. A reinforcement plan of the wooden house

Even though the soft first story type of collapse is often stressed, the failure mechanism depends on the design and physical layout of the structure, i.e., strength and distributions of columns, beams and walls. For example, Fig. 4 shows the response sequence of the two-storey wooden house. During the strong motion earthquake, the house deformed beyond the limit of linearly elastic behavior, and the eastern portion (right hand side in the figure) of the first floor began to fail at around 3 s, and collapsed at about 4 s.

In order to avoid the collapse in Figs. 4 and 5, several retrofit plans were developed such as shown in Fig. 6, where the red members indicate reinforced walls. The method proposed in this paper was then used to simulate the earthquake response of each of the reinforced houses. Results showed that the house in Fig. 6 withstood the same earthquake motions used in Fig. 5, i.e., the amplified waves of the 1995 Kobe earthquake (Figs. 7 and 8). Based on the obtained results, engineers can propose retrofit plans so house owners can improve the performance of their houses against earthquakes.



Figure 7. Comparison between the response behaviors of existing and reinforced wooden houses due to the earthquake ground motions (multiplication factor = 1.5)



Figure 8. Comparison between the response behaviors of existing and reinforced wooden houses due to the earthquake ground motions (multiplication factor = 2)

6. RELIABILITY OF SIMULATED RESPONSE

Most wooden houses in Japan are generally composed of frame units made of columns and beams, and walls. Therefore, in order to establish the reliability and correctness of collapse simulation of an entire house, it is obligatory to show the agreement of simulated and experimental results for such structural units. Fig. 9 shows frames with different types of reinforcements. A monotonically increasing force was then applied horizontally to the upper beam of each frame, and the response was computed using the same program that was used in section 5.

Based on the obtained response of the upper beam, the relationship between the displacement and force was plotted by solid lines in Fig. 10 for each frame unit (1) through (6). The experimental relationships obtained by Miyoshi et al. (2001) were also plotted by dashed lines in Fig. 10. The numerical and the experimental curves agree well including the rigidity in small strain, the maximum strength, and the weakening process, and this shows the reliability of the simulation in this paper.



- Figure 9. Samples of wooden frame units. From right to left: wooden frames with
 - (1) no end connection plate; (2) end connection plates; (3) plaster board;
 - (4) siding board; (5) two single braces, plaster board and siding board; and
 - (6) two double braces, plaster board and siding board



Figure 10. Force-displacement relationships of wooden frames

7. CONCLUSIONS

This research attempted to simulate seismic collapse of wooden houses subjected to the 1995 Kobe earthquake using the Rigid Body-Spring Method (RBSM) for the purpose of retrofitting. The following conclusions can be drawn:

- (1) The proposed method is capable of demonstrating to some extent various collapse behavior of wooden houses during strong motion earthquakes. More accurately, the link system used to characterize plastic hinges of the simplified structural components can simulate local failure that causes the entire house to collapse during strong motion earthquakes.
- (2) The method provides a way to identify the weak point of a structure thus allowing engineers to perform retrofitting analysis easily and to suggest ways to improve the seismic performance of built wooden houses.

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