



3-2-7

## ENGINEERING DURATION OF STRONG MOTION AND ITS EFFECTS ON SEISMIC DAMAGE

Li-Li XIE and Xiaozhi ZHANG

Institute of Engineering Mechanics, State Seismological Bureau of China  
9 Xuefu Road, Harbin, China

### SUMMARY

In this paper, the existing definitions of strong ground motion duration are reviewed and re-classified into two different categories: record-based duration which was directly defined upon ground motion accelerograms and response-based duration which was defined upon response of structure subjected to ground acceleration. A new definition, i.e. engineering duration of earthquake ground motion is presented and its predicting equations are deduced. It shows that the new definition can much better reflect both the characteristics of ground motion and its effects on response of structure than can any definition presented ever before.

### INTRODUCTION

It has been widely accepted that the duration of ground motion plays a significant role in causing seismic damage of structures during earthquakes. Since the earlier studies [1] on the dependence of duration on magnitude were carried out in 1960's, a number of studies on this problem have been conducted by seismologists and earthquake engineers from various angles [2-7,10]. The past studies on duration are essentially focusing on the three aspects: 1. definition and implication, 2. its correlation with other parameters, such as earthquake magnitude, distance, soil properties etc. and 3. the effects of duration on seismic damage to structures. As to the definition of duration, it is still a problem unsolved so far, though a variety of definitions have been suggested. In summary, they could be divided into two main categories: the record-based duration and response-based duration. The former was directly defined upon ground motion accelerograms and the "bracket duration" by Bolt, "fraction duration", [5, 8] Trifunac and Brady's duration, the "Second Moment Duration" by Xie and Zhou [5], Vanmarcke and Lai's duration etc. are examples of such kind. The latter was set upon the response of the single degree of freedom (SDOF) system subjected to ground acceleration [6, 7].

It is clear that a record-based duration could well correlated with seismic parameters but has nothing to do with the characteristics of structures and it is hardly to expect that a good correlation could be found between this kind of duration and severeness of structural damages. On the other hand, the existing response-based durations are very complicated in computation and rarely have seismic information involved in so that it is also very difficult to expect that an intuitive and strong correlation could be established between the response-based durations and seismic and structural parameters.

This paper is trying to define an "Engineering Duration" of ground motion which

is directly related with the main structural characteristics and has a very similar expressions with record-based duration. It's correlations with seismic parameters and effects on structural damage are also examined.

#### ENGINEERING DURATION

1. The engineering duration  $T_e$  is defined here as the elapsed time from the first to the last acceleration equal to  $a_y$  on the accelerogram as shown in fig. 1. And  $a_y$ , called Yielding Acceleration, could be expressed as

$$a_y = Q_Y / (M \times \text{BETA}(T)) \quad (1)$$

where  $Q_Y$ -the yeild strength of a given structure ( as a SDOF system),  $M$ -the total mass of the same structure, and  $\text{BETA}(T)$ -the ordinate of the response spectrum of the accelerogram corresponding to the period and damping ratio equal to the fundamental period  $T$  and the damping ratio of the given structure respectively.

2. It can be easily worked out that the engineering duration is only an extension of bracket duration given by Bolt. But a constant acceleration threshold (for examples, 0.05 g or 0.10 g adopted by Bolt) has been replaced by an important structural index  $a_y$  which represents an acceleration limit to cause the structure entering the plastic deformation stage.

This substitution brings a merit to avoid subjective arbitrariness in defining the duration of ground motion and reflect somewhat objectively the characteristics of structure.

3. The Engineering Duration gives a very clear physical meaning. If the acceleration  $a$  of ground motion exceeds the yielding acceleration  $a_y$  of the given structure, the seismic force on this structure equals  $M \times a \times \text{BETA}(T) = Q_y$  and the plastic deformation will thus appear on the structure. Obviously, for different structures, each time history of acceleration will have different engineering duration  $T_e$  i.e. will give different effects on different structures. Particularly, the engineering duration  $T_e$  will be zero in case the maximum acceleration of ground motion less than the given yielding acceleration  $a_y$ . It means that the mentioned ground motion is of no significance to damage to the given structure. Additionally, one may find that for a given structure, different ground motions will also have different engineering durations which do represent the proper characteristics of respective ground motion.

#### CORRELATION WITH MAGNITUDE, DISTANCE AND SOIL CONDITIONS

A number of prediction equations of duration has been developed in terms of Magnitude  $M$ , Distance  $R$  and soil conditions ( $s=0, 1$  and  $2$ , represents rock, moderate and soft soil respectively). For example, McGuire [8] presented the prediction equations for bracket duration  $T_b$  (0.05g) and Trifunac-Brady's 90% relative energy duration  $T_{fb}$  as

$$T_b = 9.974 e^{2.000M} \times R^{-1.270} \times e^{0.200s} \quad (2)$$

$$T_{fb} = 1.209 e^{0.150M} \times R^{0.350} \times e^{0.730s} \quad (3)$$

Also Zhou and Katayama [9] have presented the prediction equation for the Second Moment Duration  $T_{xz}$  as

$$T_{xz} = 0.253 \times 10^{0.173M} \times 10^{0.149s} \times R^{0.155} \quad (4)$$

The prediction equation of engineering duration  $T_e$  could be easily established from these existing results as shown in equations (2), (3) and (4), only if the shape of seismic energy distribution along the time axis  $a^2(t)$  could be approximately assumed as the Normal Gaussian Distribution. According to this assumption, the engineering duration  $T_e$  could be expressed in term of  $T_b$ , or  $T_{fb}$ , or  $T_{xz}$ [10], such as

$$T_e = T_b \cdot [\ln(a_m/a_y) / \ln(a_m/a_b)]^{1/2} \quad (5)$$

$$T_e = 1.26 T_{fb} [\ln(a_m/a_y)]^{1/2} \quad (6)$$

$$T_e = 2 T_{xz} [\ln(a_m/a_y)]^{1/2} \quad (7)$$

where

$a_b$  -- 0.05g, the designated acceleration level taken as the threshold for bracket duration.

$a_m$  -- the maximum acceleration of ground motion

From equations (2) and (5), (3) and (6), and (4) and (7), several prediction equations of engineering duration could be obtained from different sources [10]. They are respectively expressed as follows and illustrated in fig. 2.

$$T_e = 9.974 e^{2.000M} \times R^{-1.270} \times e^{0.200s} [\ln(a_m/a_y) / \ln(a_m/a_b)]^{1/2} \quad (8)$$

$$T_e = 1.470 e^{0.150M} \times R^{0.350} \times e^{0.730s} [\ln(a_m/a_y)]^{1/2} \quad (9)$$

$$T_e = 0.506 \times 10^{0.173M} \times R^{0.155} \times 10^{0.149s} \times [\ln(a_m/a_y)]^{1/2} \quad (10)$$

By now, three different prediction equations have been deduced by directly using the existing results developed by different authors. It is not the purpose of this paper to compare those results and indicate their implication. What should be stated is that the prediction equation of engineering duration could be directly deduced from any existing or new prediction equations developed for other record-based durations. Thus, the correlation between engineering durations and seismic parameters and soil properties could be easily established.

## EFFECTS ON SEISMIC DAMAGE AND COLLAPSE OF STRUCTURES

In order to estimate the effects of engineering duration on destructiveness and collapse of structures, a comprehensive study has been carried out for two mechanical models of SDOF nonlinear system [11]. These two models both have hysteretic force-deformation relation but model I with linearly degrading stiffness and model II with rigidity and strength cyclically deteriorated shown in fig. 3. Additionally, three different natural periods of 0.2, 0.5 and 1.0 second were taken on each model for examining the different effects on models with different rigidities. In computation, forty arti-

cially generated acceleration time-histories with 10 maximum acceleration of different levels were used as inputs. As examples, two of them are illustrated in figure 4. The engineering durations of those ground motions are ranging within 6-30 second for all SDOF system considered. As a criterion of collapse,  $u = u_c$  or  $Q_i \leq 0.2Q_y$  (only for model II) was taken into account where  $u$  is the relative displacement of SDOF system and  $Q_i$ , the ultimate strength of SDOF system after several cyclical degradation.

The computation results are shown in figure 5-6 [11] and the histograms indicate that with increasing of engineering duration the number of collapsed structures are proportionally increased. It could be believed that a very good correlation is existing between the engineering duration and collapse of structures. Engineering duration does play a significant role in causing the damage and collapse of buildings.

### CONCLUSIONS

The engineering duration of ground motion is defined directly on the ground motion accelerogram by using the important structural parameters as a threshold. It could be determined without mixing any subjective arbitrariness and has a very clear physical meaning that the only ground motion during the engineering duration will play an important role in causing damage to structures. The correlation between engineering duration and other factors could be established directly as indirectly from existing or future developed ones for other durations. From a number of nonlinear analysis, it has shown that the engineering duration is a good measure describing the severence of ground motion and its effects on the seismic destructiveness of structures.

### REFERENCES

- [1] Housner, G. W., Intensity of Shaking near the Causative Fault, Proceedings of 3rd WCEE, Vol. 1, pp. 94-109, New Zealand.
- [2] Bolt, B. A., Duration of Strong Ground Motion, 5 WCEE, Vol. 1, 1973
- [3] Trifunac, M. D. and Brady, A. G., A Study on the Duration of Strong Earthquake Ground Motion, BSSA, Vol. 65, pp. 581-626, 1975
- [4] Vanmarcke, E. H. and S. P. Lai, Strong Motion Duration and RMS Amplitude of Earthquake Records, BSSA, Vol. 70, No. 4, 1980
- [5] Xie, Li-Li and Zhou, Yongnian, A New Definition of Strong Ground Motion Duration, Earthquake Engineering and Engineering Vibration, Vol. 4, No. 2, 1984
- [6] Perez, V., Response Time Duration of Earthquake Records, 6WCEE, Vol. 1, 1977
- [7] Lu Lin, The Effects on Damage to Structure and Its Application in Engineering, A dissertation for M. D., Institute of Engineering Mechanics, State Seismological - Bureau, 1984
- [8] McGuire, R. K., The Usefulness of Ground Motion Duration in Prediction of the Severity of Seismic Shaking, 2nd U. S. National Earthquake Engineering Conference, pp. 713-722, 1979
- [9] Zhou Yongnian and Tsuneo Katayama, Effects of Magnitude, Epicentral Distance and Site Conditions on the Duration of Strong Ground Motion, SEISAN-KENKYU, Vol. 37, No. 12, 1985
- [10] XIE, Li-Li and Zhang, Xiaozhi, Accelerogram-Based Duration and Engineering Duration of Ground Motion, Earthquake Engineering and Engineering Vibration, Vol. 8, No. 1, 1988
- [11] ZHANG, Xiaozhi and XIE, Li-Li. The Effects of Engineering Duration on Seismic Damage to Structures, 1988, (in press)

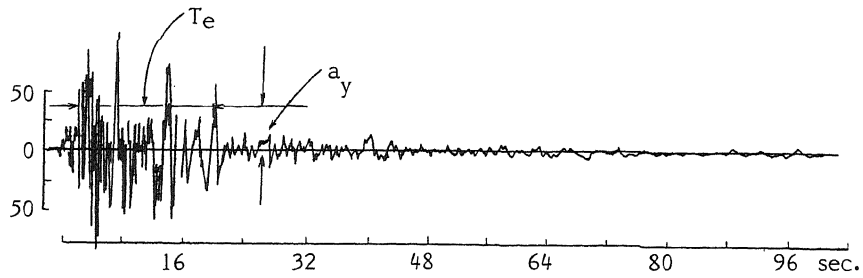


Fig.1 Definition of Engineering Duration on Accelerogram

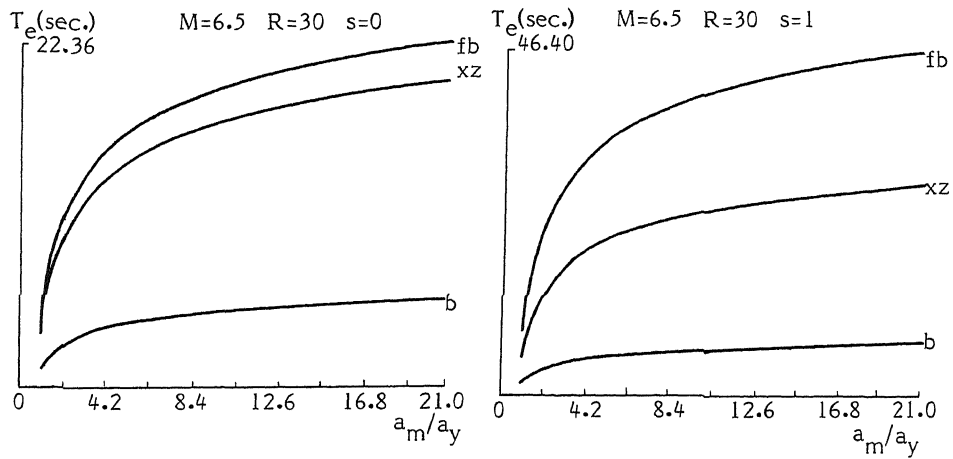


Fig.2 Regressive Curves of Engineering Duration vs. Magnitude, Distance and Soil Conditions

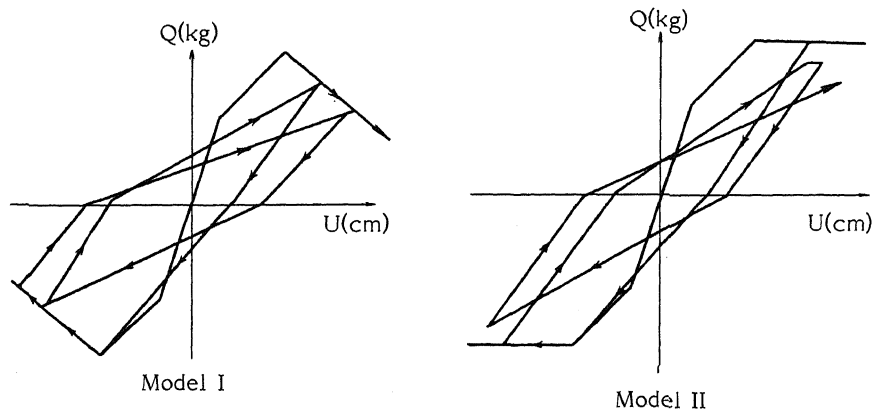
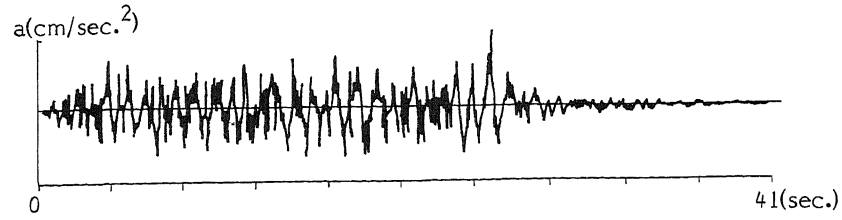
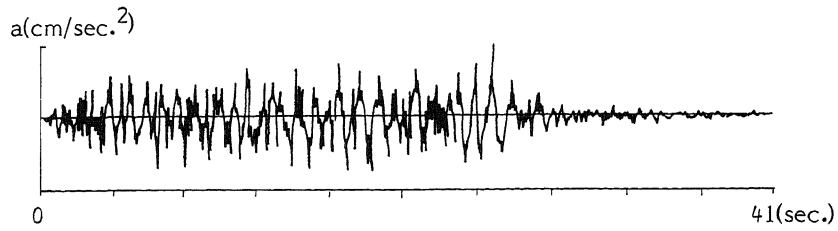


Fig.3 Curve of Restoring Force-Deformation of Model I and II



Sample 1



Sample 2

Fig.4 Examples of Artificially Generated Accelerograms used for Collapse Analysis

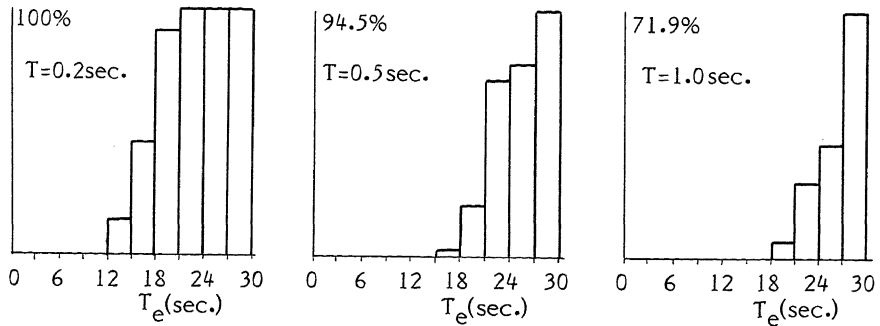


Fig.5 Histograms of Number of Collapsed Structures for Model II

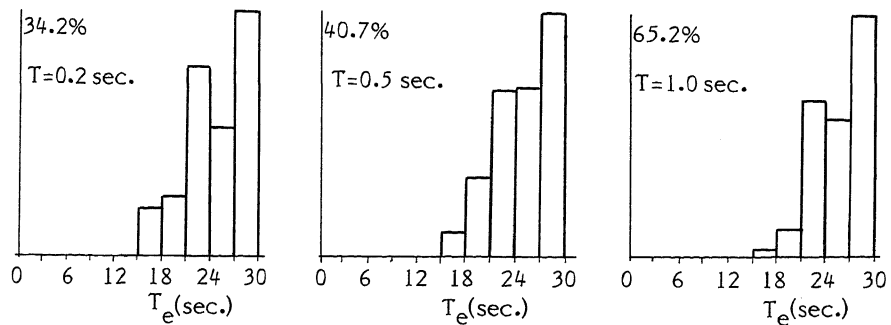


Fig.6 Histograms of Number of Collapsed Structures for Model I