## THE CAPACITY AND MECHANISM OF COUPLED SHEAR WALLS SUPPORTED BY PILE FOUNDATIONS

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#### SUMMARY

The simplified method to evaluate the characteristics of vertical restoring forces of pile foundations is proposed. The application of this method to the analysis of the capacity and mechanisms of coupled shear walls supported by pile foundations is presented.

## INTRODUCTION

The investigations of vertical displacements of pile foundations is a requirement in order to analize the behavior of superstructure constructed with shear walls during an earthquake motion(Ref. 1,2). E.D'appolonia (Ref.3) H.G.Poulos (Ref. 4), R.Butterfield (Ref. 5) and S.Yao (Ref. 6) have studied on the vertical behaviors of single piles or pile groups in the half infinite elastic media, in static terms. As an extension of the methods employed in above studies, and taking the nonlinear property of the soil rigidity into consideration, the author was able to present an analysis on single pile or pile groups which are effective to the cyclic loading phenomena. Refering to these precise analysis and field experimental data observed (Ref. 7), the simplified method to predict the vertical displacements of piles or pile groups is presented in this report (Ref. 8).

THE SIMPLIFIED METHOD TO PREDICT THE SETTLEMENTS OF PILE FOUNDATIONS

# Basic Concept

The load  $P_{O}$  acted at the pile head vertically is reacted in the ground by frictional force  $\mathbf{R}_{\mathbf{f}}$  and pile tip reaction force  $\mathbf{R}_{\mathbf{p}}$  as shown in the following eq.1.

$$P_{o} = R_{f} + R_{p} \qquad \text{or} \qquad P_{t} = R_{ft} + R_{pt} \qquad ------ \text{(1)}$$
 The settlement of pile head  $\delta$  is composed of the components  $S_{1}, S_{2}$  and  $S_{3}$ 

as shown in eq.2.

$$\delta = s_1 + s_2 + s_3$$
 or  $\delta = s_{1t} + s_{2t} + s_{3t}$  ----- (2)

As illustratively explained in Fig. 1, S1 means the compressibility of pile shaft, So means the settlement of the ground at pile tip generated by Rf and S3, the settlement of the ground at pile tip generated by Rp which acts at the same pile tip. Although  $\rm S_2$  and  $\rm S_3$  should be solved by means of half infinite space media analysis, in this methodology the simplified method as shown in Fig. 2, is presented. The original half infinite ground is substituted with the half infinite right truncated pyramid, where the calculated vertical displacement would be almost equal to that of the original. Thus, by limitting a scope of the description to a case of the pile groups, Sot indicate the vertical displacement at the pile tip, due to the compressibility of half infinite right pyramid loaded by R<sub>ft</sub> at it's truncated point. Similarly S<sub>3t</sub>

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is the vertical displacement of another half infinite truncated right pyramid at the pile tip level, due to the load  $R_{\rm pt}$  acting on the same level. The symbols used are summerized and explained in Table 1..

### Driven Piles

Driven piles give enough preloading or plastic strain to the surrounding soil of pile shaft or pile tip during it's driving process. Owing to the strain-hardening phenomena of ground materials, driven piles behave as perfectly elastic-plastic in vertical direction (Ref. 6,9). Accordingly, the following equations could be obtained in explaining the elastic state or pre-ultimate load. In this eq.  $\eta$  is an estimated constant from the ground-pile system, but it is not constant exactly. It is caused by the progressive plastic slip occurrence between soil and pile shaft surface.

## Single Pile

## Non-Displacement Piles

Compared with the driven piles, non-displacement piles (Cast in place piles or Bored piles) commonly do not give preloadings or plastic strains to the surrounding soils of pile shaft or pile tip during it's construction process, because of their peculiar construction method (Ref. 6,9). Therefor the

vertical behaviors of these piles are characterized by the strain hardening settlement in case of virgin loading. The following equations are induced to predict the settlement of non-displacement piles in considering these situations(Ref. 6). The compressibility of pile shaft is still almost elastic. In addition, the settlement component S<sub>2t</sub> or S<sub>2</sub> could be regarded as elastic because the distance between the loading level of R<sub>t</sub> or R<sub>t</sub> and the pile tip level where the settlement should be estimated, is far enough to cause the stress due to R<sub>rt</sub> or R<sub>r</sub> to dissipate to small stress distribution level. So S<sub>1</sub> and S<sub>2</sub> for non-displacement piles are exact same formulae as S<sub>1</sub> and S<sub>2</sub> in eq.3 and eq.4 for the driven piles. On the settlement component S<sub>1</sub> or S<sub>2</sub>, the strain hardening behavior should be taken into account, as shown in the followings (Ref. 10).

Single Pile

S<sub>3</sub> = S<sub>3e</sub> + S<sub>3pr</sub> (5)

Where, S<sub>3e</sub> is a purely elastic component which is the same S<sub>3</sub> given in eq.3.

S<sub>3pr</sub> is a plastic settlement component resulted from the strain hardening rule of soils near the pile tip and takes the quadric form of P<sub>0</sub> as follows (Ref.6,10).  $S_{3pr} = \frac{4.9 \, n^2 \, P_0^2}{R_{pu} \, \pi \, E_S \, D}$ (6)

$$S_{3pr} = \frac{4.9 \, \eta^2 \, P_O^2}{R_{DU} \, \pi \, E_S \, D} \qquad ---- \qquad (6)$$

Eq.6 is valid only when  $P_{O}$  is a virgin load.

Pile Groups

As for the settlement component S, in case of pile groups, the term S, is added to the right side of eq.5 for single piles. Thus it takes the following form eq.7.

$$s_3 = s_{3e} + s_{3pr} + s_{3Br}$$
 (7)

The terms  $S_{3e} + S_{3pr}$  in the right side of eq.7 are exact the same as those of eq.5. The new term  $S_{3pr}$  means the plastic settlement component resulted from the strain hardening rule of soils as observed block settlement behavior of pile groups near pile tips and it takes the quadric form of  $P_{+}$  as described in the following eq.8.

$$S_{3Br} = \frac{6\eta^{2} \cdot P_{t}^{2} \log \frac{1_{yo}}{1_{xo}}}{2R_{ptu} \cdot E_{s} (1_{yo}^{-1}_{xo}) \tan \alpha}$$

$$= \frac{6\eta^{2} \cdot P_{t}^{2}}{2R_{ptu} \cdot E_{s} \cdot 1_{o} \tan \alpha} \quad (if \ 1_{xo}^{-1}_{yo}^{-1}_{o})$$

These components expressed by eq.6 and eq.8 are also illustrated in Fig.3, where the shaded zone in Fig. 3(a) shows nonelastic but strain hardening zone which induce the penetration settlement and the shaded zone in Fig.3(b) the similar zone for the block settlements (Ref. 6). In case of unloading process, the nondisplacement pile also shows the perfectly elastic behavior. Therefor  $\Delta S_3 = \Delta S_3$ , that is  $\Delta S_3 = 0$ , in eq.7, where  $\Delta S_3 = 0$  in eq.7, where  $\Delta S_3 = 0$  in eq.7, where  $\Delta S_3 = 0$  in eq.7 tend ty of each component. to give almost upper limit of the plastic settlement quantity of nondisplacement piles compared with many field data which locate generally between the curves given by eq.3 and eq.4 and the curves given based on eqs.5 or 7, if the reasonable constants are employed as shown in the following paragraph.

## Settlement Rigidity k

The analysis of pile-superstructure system could become available by employing an application of the load-settlement relations mentioned above. In conducting the analysis, the settlement rigidity of pile head k= $P_0/\delta$ or  $P_t/\delta$  would be useful. As an example of actual use of eq.3 or eq.4 of driven piles, the author recommends the following constants, a=0.5,  $\nu$ =0.4, L'=1/3,  $\alpha$ =40°. Thus, from eq.3 and eq.4, k is derived as follows.

$$\frac{1}{\frac{\text{Single Pile}}{k}} = \frac{\delta}{\frac{\delta}{p_0}} = \frac{(1+\eta)L}{2E_p \cdot A_p} + \{0.484(1-\eta) + 0.093 \frac{\eta}{\bar{d}}\} \frac{1}{G_s \cdot L} --(9)$$

$$\frac{1}{\frac{\text{Pile Groups}}{k}} = \frac{\delta}{\frac{1}{p_t}} = \frac{(1+\eta)L}{2m \cdot E_p \cdot A_p} + \{\frac{(1-\eta)}{2.629+1.677\bar{l}_0} + \frac{\eta}{4.70\bar{l}_0}\} \frac{1}{G_s \cdot L} --(10)$$

where,  $\eta$  =0.2 is to be recommended when Po is small, and  $\eta=(P_O-R_{\tilde{L}_U})/P_O$  when  $P_O\geq P_f$ . To estimate the ultimate strength of a pile, following formulae are recommended in Architectural Institute of Japan (AIJ).  $30\cdot \bar{N}\cdot A_D+(N_S\cdot L_S/5+q_U\cdot L_C/2)\cdot \psi$  tf for pushing down, and  $(N_S\cdot L_S/5+q_U\cdot L_C)\cdot \psi$  tf for pulling up, where  $\bar{N}:SPT$  N value around pile tip,  $N_S:SPT$  N value of intermediate sandy layer of thickness  $L_S$ ,  $q_U:uniaxial$  strength of intermediate clay layer of thickness  $L_C$ ,  $\psi:$  perimeter of pile shaft. In this report, these formulae are recommended to be available for both driven piles and nondisplacement piles, and the ground elastic constants  $G_S=100.N$  tf/m²(N:SPT N) for sandy layer,and  $G_S=50.Z$  tf/m² (Z:depth in meters from G.L.) for normally consolidated clay, could be recommended (Ref. 11).

## BEARING CAPACITY AND RESTORING FORCE CHARACTERISTICS OF PILE FOUNDATION

The above mentioned vertical behaviors of piles are resulted from soil mechanics characteristics, but in estimating the overall strength of pile foundation, the strength of pile shaft or other parts should also be taken into accounts. Fig. 4 shows the axial forces (P) - bending momement (M) - (shearing forces) interactive curve of a pile shaft member. After the analysis of combined stress condition in pile shaft, the ultimate axial strength should be obtained from Fig. 4. The pulled up strength of a pile caused from soil-pile surface shear strength would be near  ${\tt R}_{{\tt fu}},$  and the isotropic hardening rule with respect to pile surface shear behavior is to be assumed, then the displacement characteristics of pulled up piles could be the same as pushed down piles under the load  $P \le P_f^{'}$  . In table 2, some critical loads at pile head are summerized and defined, which are important in considering the characteristic restoring forces of piles. At each critical load, the supporting mechanisms would somewhat change, accordingly the vertical displacement characteristics would also change. In Fig.5, a diagram on the vertical characteristics of restoring forces is illustrated. As shown in Fig.5, the load at pile head generated by seismic load Q should start from the point of the long term reaction force  $P_{\mathrm{L}}$  on abscissa of Fig.5.

# THE CAPACITY AND DEFORMATION OF PILE - COUPLED SHEAR WALL SYSTEM

Two coupled shear walls with coupling beams which are plane symmetry have been analysed as shown in Fig.6. The symbols used in the analysis are summerized in table 3. The fundamental equations are as follows which are the equibrium equations of vertical forces and moments(eq.11) about the half left of Fig.

6 and the constitutive relations (eq.12). Equations are formed under the intial condition where long term load W is working.

 $\begin{array}{c} R_1 + R_2 + \Sigma \ 2M_1/1 = 0. & Q \cdot H + R_1 \cdot L - \Sigma \ M_i = 0. & ------ \ (11) \\ M_i = K_{Bi} (\theta - R)/2 & M_i \leq M_i, R_j = k \cdot \delta_j, R_j \leq R_{ju} \\ \text{where} & 1/K_{Bi} = 1/K_{mi} + 1/K_{Si} & K_{mi} = 12E \cdot K_i \\ \end{array}$ 

The assumptions on this analysis are the followings. Coupling beams and pile foundations behave as perfectly elastic-plastic and shear walls as rigid-plastic. Seismic load distributions are substituted with a equivalent total load 2Q which acts at an equivalent level H from the ground level. Coupling beams behave as bending members being dominant, therefor  $K_{B_1} = K_{M_1}$ . The examined ground profile is shown in Fig.7, and the constants of the ground,piles and superstructures are summerized in table 4 and 5. For simplisity,  $k_1 = k_2 = k$ . The Results of Analysis

The results of case I (for steel pile) and case II (for prestressed concrete pile) are shown in Figs.8 and 9. In both cases, the first yieldings occur at the footing beam and the second yieldings occur at the coupling beams. These are shown as breaking points Y1 and Y2 in the figures. The last yielding that is the formation of failure mechanisms, occurs at the pushing down pile (R1) in case I, and at the pulling up pile(R1) in case II where the tensile collapse of P.C. pile has occured. In case I, before getting this capacity load the yielding of shear walls should also be taken into account. To complete these mechanisms, some ductility of beam flexure should be required as shown in Figs. 8 and 9 with respect (0-R). The ratio  $\phi=K_{\rm B}/K_{\rm F}$  could be important parameter in the analysis, where  $K_{\rm B}$  is the total rigidity of coupling beams and  $K_{\rm F}$  is the rocking spring constant of the isolated cantilever wall. The symbols are summerized in table 6. The elastic deformations obtained are

From eq.13,the deformation modes of this structure can be classified as shown in Fig.10 according to the formula  $\frac{1-\alpha\varphi}{}$ . When  $1-\alpha\varphi\geq 0$ . the independent rocking, and when  $1-\alpha\varphi\leq 0$ . the entire rocking of this structure will be predicted. From substituting unit with the left sides of eqs.14,that is  $Q_{um}/Q_{u1}=Q_{um}/Q_{u1}=Q_{un}/Q_{u2}=Q_{um}/Q_{um}=1$ ., the discriminants can be obtained, using the critical strength ratios of members (CR1  $\sim$  CR4) defined in eqs.14 as foll—

$$R_{1u} \cdot L/m \cdot M_{iu} = CR_{1} , R_{2u} \cdot L/m \cdot M_{iu} = CR_{2} R_{2u} / R_{1u} = CR_{3} , M_{ou} / m \cdot M_{iu} = CR_{4}$$
 } ------ ( 15 )

If all of the four equations in eqs.15 are valid, it means that all members reach yielding simultaneously and at the same time the system forms the failure mechanism. Usually, various other cases are presumed based on eq.15. For an example, if  $R_{1u}\cdot L/m\cdot M_{\phantom{1}u} < CR_{1}$  is valid, it means that the yielding of rocking moment resulted from the ultimate strength of pile foundation (  $R_{1u}$  ), occurs earlier than the yielding of coupling beams, that is the pseudo strong beam – weak foundation system. And the inverse sign of inequality

means the pseudo strong foundation - weak coupling beam system.

#### CONCLUDING REMARKS

The simplified method to predict the characteristics of restoring forces of pile foundations was proposed and an application of this method was presented.

The discriminant for deformation modes of coupled shear wall structure was 1-  $\alpha\phi$ , and the usefulness of critical strength ratio CR<sub>1</sub>, CR<sub>2</sub>, CR<sub>3</sub>, CR<sub>4</sub> was discussed using eq.15.

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Table 1. Definitions of Symbols
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                 (for input data)
                                                                      ( Capital P means the load acting on
 Ap : net area of pile shaft section
                                                                        one pile in the foundation where
    : pile diameter
                                                                        the reacting forces R_1 or R_2 are
 L : embeded length of pile
                                                                        acting )
    : distributing factor of
                                                                      P1 : long term load
       frictional stress Rf
                                                                      P_{\mbox{\scriptsize pc}}^{-}\colon ultimate compression strength
 L' : distance of equivalent loading
                                                                            of pile shaft
       point of R_f or R_{ft} from pile
                                                                      P_{\mbox{pt}}: ultimate tention strength
        tip
                                                                            of pile shaft
 \boldsymbol{\eta} : load transmitting factor at
                                                                      P_f: P under the condition of R_f = R_{fu}
   pile tip, R_p/P_0 or R_{pt}/P_t: number of piles in pile groups
                                                                      P<sub>1</sub>: P under the condition of R<sub>p</sub>=R<sub>pu</sub>/3
P<sub>2</sub>: ultimate bearing capacity of P
 l_{x_0}, l_{y_0}: scale of perimeter of pile
                                                                      ( R_{\mbox{\footnotesize f}} = R_{\mbox{\footnotesize f} u} and R_{\mbox{\footnotesize p}} = R_{\mbox{\footnotesize p} u} ) P_{\mbox{\footnotesize f}} : ultimate bearing capacity of P
              groups
 Ep : young's modulus of pile material
                                                                             of up lift (Rf=Rfu and Rp=0.)
 Es : young's modulus of ground soil
 V : poisson's ratio of ground soil
Po,Pt: load at pile head
Rf,Rft: total frictional force
Rp, Rpt: reacting force at pile tip
                                                           Table 4. Input Data for piles
Rpu,Rptu :ultimate strength of Rp
or Rpt
Rfu,Rftu :ultimate strength of Rf
                                                                      Case I Case II
                                                                     0.016 , 0.181 m<sup>2</sup>
                                                                                            Table 5. Input Data for system
                                                                     0.6 , 0.6 m
21. , 4. x10<sup>6</sup>t/m<sup>2</sup>
             or Rft
S<sub>1</sub>,S<sub>2</sub>,S<sub>3</sub> :refer to Fig.1
                                                                  : 21.
                                                                                      t/m<sup>2</sup>
   : vertical displacement of pile
                                                                         25.5
1.5
3 piles
                                                                                                       :
                                                                                        m
      head
                                                                                                           9 stories
6.94 x10<sup>-3</sup>m<sup>3</sup>
2.31 x10<sup>-3</sup>m<sup>3</sup>
                                                                                                    Ko:
Kn:
E:
Mou:
   : angle of leaning in Fig.2
\bar{d} : d/L
                                                                         0.2
                                                                                              K1 ~
Ī<sub>o</sub> : l<sub>o</sub>/L
L' : L'/L
                                                                         209.
                                                                         339.
                                                            Riu
                                                                 : 1646. for pushing tf
                                                                                             M<sub>lu</sub>~
                                                            (m=3) 627. for pulling tf
R2u: 1646. for pushing tf
 ( subscript t means the case of
                                                                  627. for pulling tf

501. , 1000. tf

501. , 100. tf
   pile groups )
                                                            (m=3)
                                                            Fpt
k
                                                                     501. , 100. <sub>4</sub> tf
2.46 , 3.01 x10 t/m
       Table 3. Definitions of Symbols
R1,R2: reaction force on pile foundation
R_{1u}, R_{2u}: ultimate strength of R_{1}, R_{2}
Mi : end moment of coupling beam i
                                                                              Table 6. Definitions of Symbols
       ( i=0. means the footing beam )
                                                                      K_F = k \cdot L^2
Miu: ultimate strength of Mi
   : holizontal seismic load
                                                                      K_B = 12E \cdot \overline{K}
                                                                                           (\bar{K} = \Sigma K_1)
H : the level where Q acts
n : number of floors of building
L,1: space of span of building in Fig.6
                                                                      \Theta_{O} = Q \cdot H/K_{F}
m : number of coupling beams which
                                                                      \mathbf{Q}_{\mathbf{Um_{1}}} : critical load of Q when coupling
       have the same Ki
                                                                               beam i yield with Miu
   : rocking angle of coupled shear wall
                                                                      Qumo : critical load of Q when footing
R : rotation angle of coupling beams
                                                                               beam yields with Mou
E : young's modulus of coupling beams
                                                                      \begin{array}{lll} Q_{UM} & : \mbox{ minor one of } Q_{Umi} \mbox{ and } Q_{Umo} \\ Q_{Ul} & : \mbox{ critical load of } Q \mbox{ when pile} \end{array}
\delta_1, \delta_2: vertical displacement of pile
           foundation, downwards as positive
                                                                               foundation yields with Rlu
Ki : rigidity of coupling beam i
                                                                      Q_{u2} : critical load of Q when pile
k1,k2 : displacement rigidity of pile
                                                                               foundation yields with R_{2u}
           foundation
                                                                           : capacity of Q due to failure
                                                                      Q_{\mathbf{u}}
\alpha : L/1
                                                                               mechanism of system
K_{mi}, K_{si}: bending or shearing rigidity
              of coupling beam i
K<sub>Bi</sub>: refered to eq.12
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