

# DYNAMIC AND STATIC TEST OF MODEL PILES OR PILE GROUPS

by

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## SYNOPSIS

The present report is concerned about the results of the experiments where the model piles or pile groups driven into clay layer have been laterally loaded both statically and dynamically. Following matters are mainly discussed. 1.) Availability and unavailability of static loading test in lateral direction, for the aseismic design concepts. 2.) Influence of pile foundations on the dynamic characteristics of superstructure, in frequency and amplitude. 3.) Dynamical modelling of ground-pile-building system and its simulate calculation.

## INTRODUCTION

In the case of pile-supported building which has the basement floor, the base shear forces would be mainly reacted by the underground walls or footing slab surfaces but not so much by pile heads. But in the case of pile-supported building which has no basement floor, the base shear forces would be almost reacted by piles. In such cases, unless the magnitude of seismic loads acting on the pile shafts is correctly estimated, piles could be greatly damaged and these damages might possibly lead to the fatal destruction of the entire building, including the overturning of tall building. There are fairly many cases of buildings supported by bearing piles where upper parts of piles protrude from the ground surface and where there exists void space between the footing slab and the ground surface as pierot'i, resulting from the consolidation settlements of alluvial clay deposit by pumping up. Taking these situations into consideration, the aseismic design philosophy for pile foundations could not be sufficient at present, especially with P.C. piles lacking in ductility.

## OUTLINE OF EXPERIMENTS

Testing Apparatus Scheme of the testing apparatus is shown in Fig. 1 and additional explanations are as follows. 1.) At the bottom of clay layer in the soil box, various frequencies of sine waves are transmitted through the vibratory table which is equipped with the vibration generator. The soil box has light rotative walls which hold the clay layer in vibratory direction, to avoid both the unnatural confinement of soil movements and the excessive dynamic inertia reactions from rotative walls. 2.) The clay layer is enclosed by the vinyl plastic sheets and glycerin to contain pore water and to cut the frictional resistance between the soil and soil box. 3.) Model piles are aluminous pipes ( 10.mm diameter. 1.mm thick, Young's modulus  $E_p=7.58 \times 10^5 \text{kg/cm}^2$ , sectional inertia  $I_p=2.89 \times 10^{-2} \text{cm}^4$ ). 4.) Steel mass and Televibrometer of 31.kg total weight, corresponding to one third of vertical ultimate strength of group piles, are fixed on the footing. 5.) Results of cone tests and vane tests in clay layer are shown in Fig. 2. Contents of Experiments Contents of experiments are shown in Table 1. as NO.1,2,3,etc..

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## RESULTS OF EXPERIMENTS

Test NO.1 Vertical ultimate bearing capacity is about 9.kg f. per one pile.

Test NO.2 Fig. 3 shows the lateral load-displacement relations obtained at pile-tops in the static tests. Fig. 4 shows the bending strain distributions in depth of each pile where the maximum bending has been observed at the corner pile and the minimum at the center pile. Group effects about displacement and bending moment are recognized in these figures. Comparing these observed bending moments with Chang's solution [1], the lateral coefficient of soil reaction  $K_h$  could be estimated and employed as  $K_h = 1.0 \text{ kg/cm}^3$  in this report.

Test NO.3 Fig. 5 shows the p- $\delta$  relation in the lateral direction at the top of rotative walls that hold clay layer. Fig. 6 shows the bending strain distributions of piles just only by the forced shear deformation of clay layer such as in Fig. 5. Bending strains observed here could be considered to be fairly small in the relative importance in seismic interaction.

Test NO.4, NO.5, NO.6 Figs. 7, 8 and 9 show respectively the dynamic response ratio spectra of each single pile obtained from the bending strains and the acceleration measurements. Fig. 10 shows the absolute acceleration spectra in clay layer measured by sensors GA1-GA4.

Test NO.7 Fig.11 shows the dynamic strain distributions along the pile shafts for the typical frequencies ( $N=5,8,19$  and  $34 \text{ Hz}$ ). Fig. 12 shows the dynamic response ratio spectra of each pile. Fig.13 also shows the dynamic response ratio spectra about the acceleration and displacement obtained from the tele-vibrometers that are setted on the footing (TV1) and on the vibratory table (TV2).

Test NO.8 Test situations are the same as those of Test NO.7 except that the level of pile head is G.L.+0. ie.H=0.. Fig.14 shows the dynamic response ratio spectra.

Test NO.9 Fig.15 shows the dynamic response ratio spectra. Fig.16 shows the absolute dynamic axial strain spectra by rocking movements.

### SOME CONSIDERATIONS ABOUT EXPERIMENTAL RESULTS

Natural Frequency of Superstructure ( $N_s$ ) In order to estimate the influence of pile foundation upon the natural frequency of superstructure, a single degree of freedom system for the superstructure is employed,

that is :  $N_s = \frac{1}{2\pi} \sqrt{\frac{K_s}{W_s}}$ , where  $W_s$  is the effective mass of superstructure and  $K_s$  is the spring constant including the influence of pile foundation.

Following equation (1) would be available for estimating the influence of pile foundation upon  $K_s$ .

$$\frac{1}{K_s} = \frac{1}{K_p} + \frac{1}{K_b} \quad (1)$$

where  $K_p$  is the spring constant due to pile foundation and  $K_b$  is the spring constant of building.

Every observed response spectrum has generally two peaks, one of which coincides with the natural frequency of superstructure including the influence of pile foundation measured in the free vibration test ( $N_{sm}$ ), and the other of which coincides with the natural frequency of clay layer measured in the free vibration test ( $N_{gm}$ ).

Now, as shown in Fig. 17, piles are assumed to be free standing on the

perfectly rigid virtual base at the level of  $-L_m$  from the ground surface. Natural frequency of the superstructure in this assumption is calculated as follows ( $N_{sc}$ ),

$$N_{sc} = \frac{1}{2\pi} \sqrt{\frac{K_p}{W_s}} = \frac{1}{2\pi} \sqrt{\frac{a \cdot E_p \cdot I_p}{(L_m + H)^3 \cdot W_s}} \quad (2)$$

here  $a=3$ . when the pile head is hinged,  $a=12$ . when the pile head is perfectly rigid and  $K_p = \infty$  in these model experiments.

The calculated  $L_m$ , which satisfies  $N_{sc} = N_{sm}$ , could be recognized to be nearly equal to or a little larger than the depth where the maximum bending moment of pile shaft is observed in case of pin-connected pile head. According to these experimental facts and also following to the fact that the ground and piles behave almost identically with each other except the vicinity of pile head, e.g. [2], the author proposes to estimate  $L_m$  using Chang's solution [1] as follows,

$$L_m = \frac{1}{\beta} \tan^{-1} \left( \frac{1}{1 + 2\beta H} \right) \quad (3)$$

where  $\beta = \sqrt[4]{\frac{E_s}{4E_p \cdot I_p}}$ ,  $E_s = K_H \cdot B$ ,  $B$  is the width of pile shaft,  $H$  is the protruding length of pile head as shown in Fig. 17.

$N_{sc}$  which is obtained from Eqs. 2 and 3, and  $N_{sm}$  which have been measured are shown in Table 2. in comparison.

Natural Frequency of Clay Layer In order to estimate the natural frequency of clay layer, the following examinations 1.) - 5.) have been tried.

1.) From empirical equations  $V_s = 60 \cdot q_u^{0.36}$  (m/sec),  $q_u = 1/5 q_c$  where  $V_s$  is the shear wave velocity in the ground and  $q_c = 3 \cdot \text{kg/cm}^2$  from the cone test results (Fig. 2), the dynamic shear modulus  $G_s$  is obtained as follows.

$$G_s = \rho V_s^2 \quad (4)$$

where  $\rho$  is the mass density of the ground.

2.) The natural frequency of elastic layer of thickness  $H_g$  for shear translation ( $N_g$ ) is given by  $N_g = V_s / 4H_g$ . Substituting for this equation the measured natural frequency  $N_{gm} = N_g$  ( $\doteq 20 \text{ Hz}$ ) and  $H_g$  ( $= 54 \text{ cm}$ ),  $V_s$  is obtained, and then from Eq. 4  $G_s$  is obtained.

3.) As illustrated in Fig. 18, the shear translation of clay layer could be modelled as a single degree of freedom system. Then the following equations are obtained.

$$N_{gc} = \frac{1}{2\pi} \sqrt{\frac{K_g}{M_g}} \quad (5)$$

Where, spring constant of the ground layer  $K_g$  is as follows,

$$K_g = \frac{A}{H_g} G_s \quad (6)$$

and  $M_g = \frac{H_g \cdot A}{2 \cdot g} \gamma_s$ ,  $A$  is the sectional area of soil layer and  $\gamma_s$  is the unit weight of soil, referring to Fig. 18.

Equating  $N_{gc} = N_{gm}$  in Eq. 5,  $K_g$  is obtained, and then  $G_s$  is also obtained from Eq. 6.

4.) Searching out the maximum modulus of rigidity from the  $p-\delta$  relation in Fig. 5,  $K_g = \left. \frac{\Delta p}{\Delta \delta} \right|_{\max}$  ( $\doteq 833 \cdot \text{kg/cm}$ ) is obtained, and by Eq. 6

$G_s$  is also obtained.

5.) Using  $K_h$  ( $= 1. \text{ kg/cm}^3$ ) applied to Chang's solution,  $G_s$  would be estimated abbreviately as follows,

$E_s = K_h \cdot B = 1. \text{ kg/cm}^2$ , where  $B = 1. \text{ cm}$ . Assuming  $E = E_s$ ,

$$G_s = \frac{E}{2(1+\nu)} \quad (\doteq 0.36 \text{ kg/cm}^2)$$

where  $\nu$  is the Poisson's ratio.

$G_s$ ,  $K_g$  and  $N_{gc}$  obtained in the above methods 1.) - 5.) are shown in Table 3.. Methods 1.) - 4.) could be recognized to be fairly reasonable, considering some other relative situations. The result of method 5.) shows that  $K_h$  applied to Chang's solution owing to the static test cannot be applied to the dynamic phenomena of the ground.

As a reason of this, the disturbance of clay or the growth of small vacancy between clay and pile surface, by the repeated movement near the ground surface, could be presumed. In Fig. 8 these phenomena could be also observed indirectly comparing with the response before and after resonance. Vibrating Modes Response spectra could be characterized by the relative magnitude of  $N_g$  and  $N_s$  as shown in Figs. 7 and 9. Vibrating modes of ground-pile-building system obtained by observing the phases of recorded waves are illustratively shown in Fig. 19 with the characteristic zoning symbols  $I_s$ ,  $II_{sg}$ ,  $III_g$ ,  $I_g$ ,  $II_{gs}$ ,  $III_s$  in Figs. 7 and 9. In Fig. 19, there are also shown the calculated modes of two-degree of freedom system employing the model which is composed of those shown in Figs. 17 and 18.

Input Shear Forces at Pile Head In order to examine the fundamental seismic input data at pile head, the response amplitude ratio spectra were obtained from the dynamic tests and also from the simulate calculation employing the two-degree of freedom system. The damping ratios  $h_g$  of the ground and  $h_s$  of the superstructure were employed referring to the observed waves of free vibrating tests. When  $N_s$  and  $N_g$  are close, the response around resonant frequency shows the drastic increase as shown in Fig. 8.

Axial forces by rocking movements in Fig. 16 are presumed ~~convently~~ by the overturning moment calculated from the center of gravity of superstructure and measured accelerations within the limits of  $N < N_s$ .

Dynamic pile group effect about the shear force distributions at pile heads does not necessarily coincide with the static one as shown in Fig. 12.

#### CONCLUDING REMARKS

The influence of pile foundation upon the superstructure which has no basement floor, in the earthquake response, could be estimated approximately by Eqs. 1 and 2, and be estimated availably also by the lateral pile-loading tests in site.

The dynamic behavior of the ground-pile-superstructure system could be fundamentally explained by two-degree of freedom system mentioned in this report.

Dynamic characteristics of the ground or of pile group effect cannot be presumed from the static loading test of piles in lateral direction.

#### REFERENCES

- [1] Chang, Y.L. (1937) : Discussion on "Lateral pile-loading Tests" by Feagin, Trans., ASCE, P272-278
- [2] Sugimura, Y. (1977) : Earthquake Observation and Dynamic Analysis of a Building Supported on Long Piles, Proc. of 6th WCEE, VOL. II, P1570-1575

Table 1. Contents of Experiments

Test NO.	Pile	H (cm)	$W_p$ (kg)	Loading	Measurement
NO.1	9Gr.Pin.& Single P.	6.	-	Static	Axial Forces Settlements
NO.2	do.	6.	-	Static	Bending strains Displacements
NO.3	9Gr.Pin.	6.	-	Static	do.
NO.4	Single p.	7.7	3.1	Dynamic	Dynamic spectra Natural freq.
NO.5	do.	4.9	0.63	Dynamic	do.
NO.6	do.	3.8	0.31	Dynamic	do.
NO.7	9Gr.Pin.	6.	31.	Dynamic	do.
NO.8	dc.	0.	31.	Dynamic	do.
NO.9	9Gr.Fix.	0.	31.	Dynamic	do.

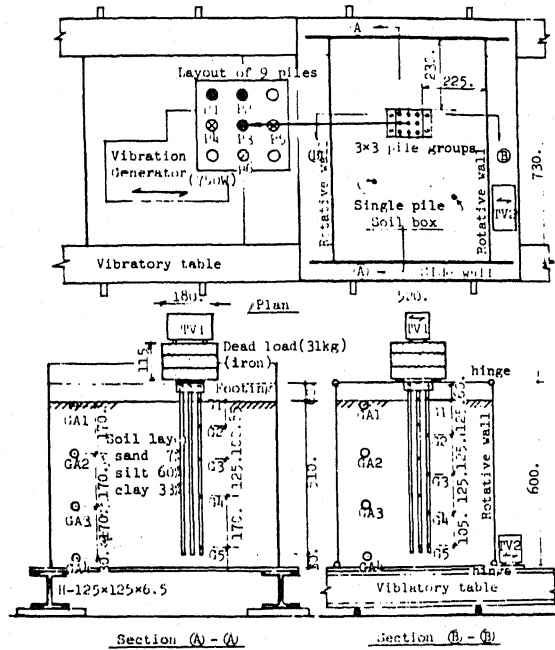
notes; H,  $W_p$  : shown in Fig.17  
 9Gr. : 3 x 3 Group Piles  
 Pin. : Pin-connected at Pile Head  
 Fix. : Fixed at Pile Head

Table 2. Measured and Calculated  $N_s$

Test NO.	$N_{sm}$ (Hz)	$N_{sc}$ (Hz)
NO.4	10.	11.3
NO.5	23.	28.8
NO.6	40.	42.7
NO.7	8.5	11.7
NO.8	13.5	13.9
NO.9	22.	27.7

Table 3. Examined Results for Clay Layer

Examined method	$C_u$ (kg/cm <sup>2</sup> )	$K_u$ (kg/cm)	$N_{sc}$ (Hz)
1.)	41.8	2939.	21.1
2.)	33.	2330.	18.8
3.)	37.6	2640.	20.
4.)	29.	2039.	17.6
5.)	0.36	25.3	2.



Symbols GA1-G3 : Strain gauges of each pile  
 GA1-GA3 : Acceleration sensors in soil layer  
 TV1, TV2 : T-D-Vibrometer (acceleration & displacement)

Fig. 1 Scheme of Testing Apparatus

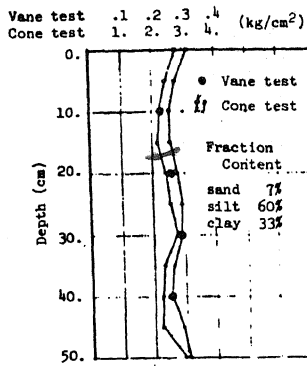


Fig. 2 Soil profile

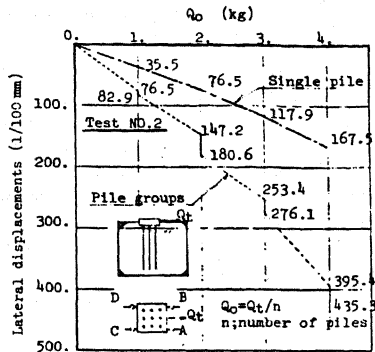


Fig. 3 Lateral loading test

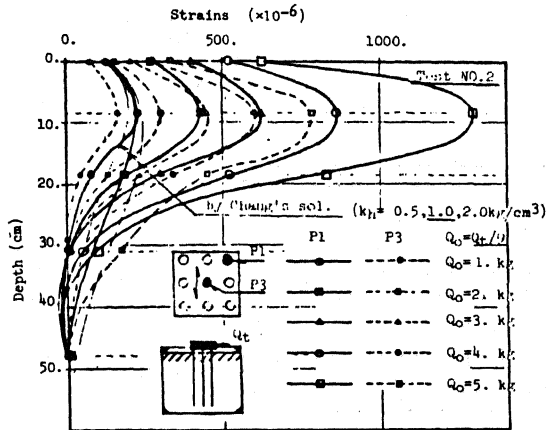


Fig. 4 Bending strain distributions in static test

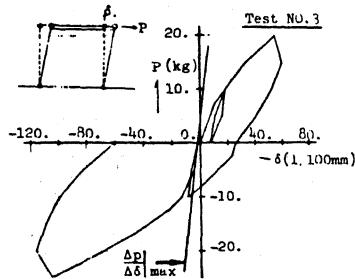


Fig. 5 Lateral load (p)-displacement (delta) relation at the top of rotative wall

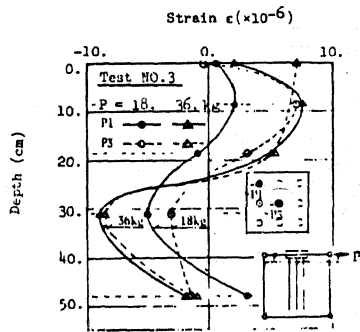


Fig. 6 Bending strain distributions of piles when rotative wall is laterally loaded by P at the top

Damping factors are evaluated in two cases as  
 ①  $h_b = \frac{18}{2\pi N_g}$ ,  $h_s = \frac{18}{2\pi N_s}$  and ②  $h_b = \frac{24}{2\pi N_g}$   
 $h_s = \frac{24}{2\pi N_s}$  in Figs. 7, 8 and 9.

$a_t$  is the acceleration evaluated from the strain of G1 at the level of ground surface.  
 $a_b$  is the acceleration measured by GA4 at the bottom of soil layer.

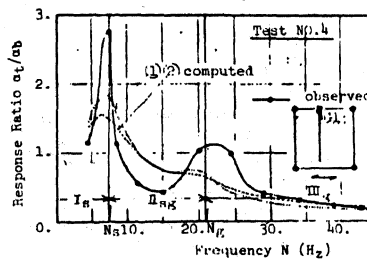


Fig. 7 Acceleration response ratio spectra

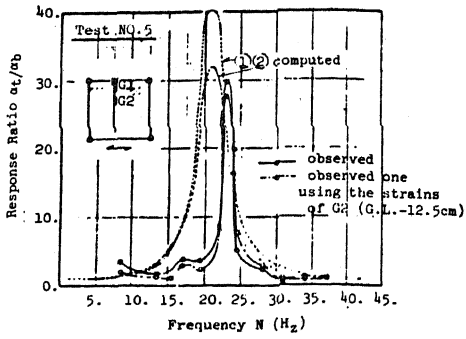


Fig. 8 Acceleration response ratio spectra

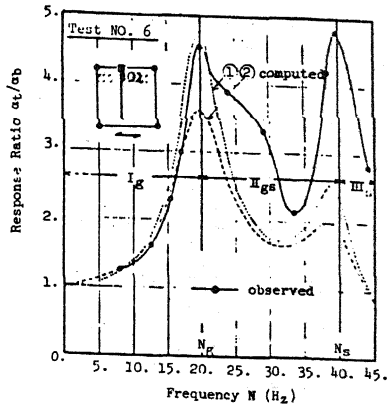


Fig. 9 Acceleration response ratio spectra

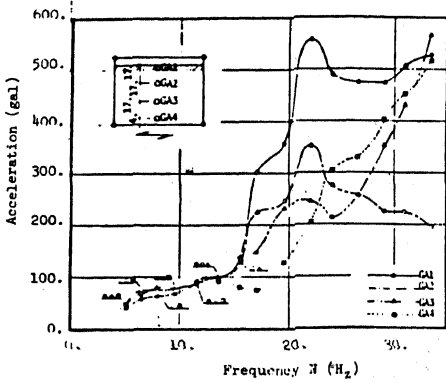


Fig. 10 Absolute acceleration spectra in soil layer

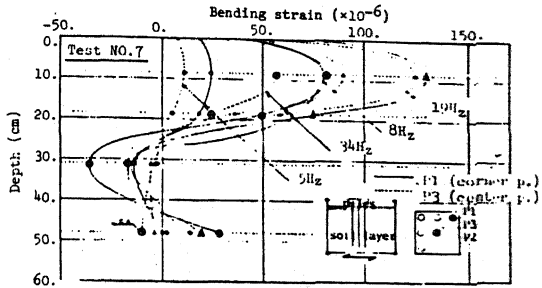


Fig. 11 Bending strain distributions along pile shafts obtained in dynamic tests

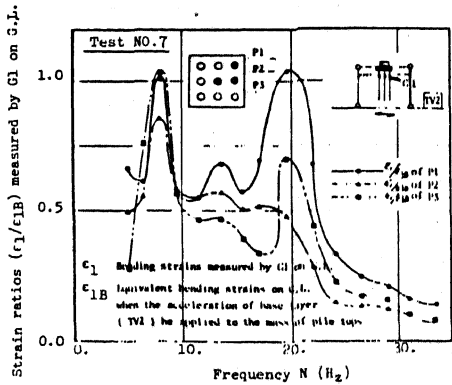


Fig. 12 Strain ratio spectra

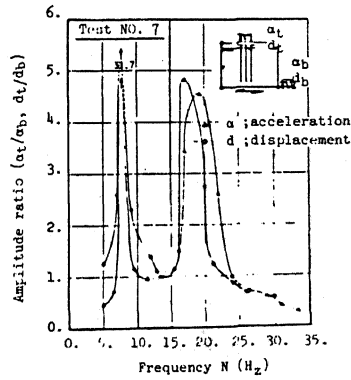


Fig. 13 Amplitude ratio spectra by Tele-Vibrometers TV13TV2

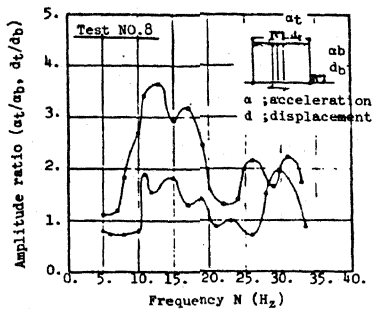


Fig. 14 Amplitude ratio spectra by Tele-Vibrometers TV1, TV2

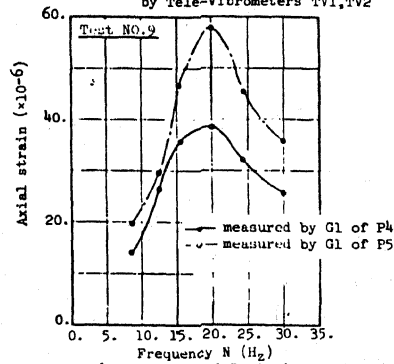


Fig. 16 Absolute axial strain spectra by rocking movement

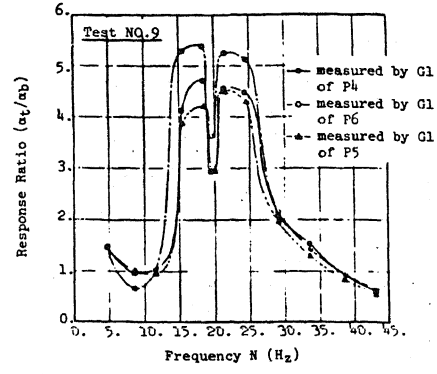


Fig. 15 Acceleration response ratio spectra

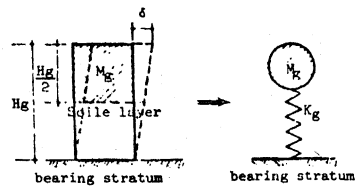


Fig. 18 Modelling of the ground

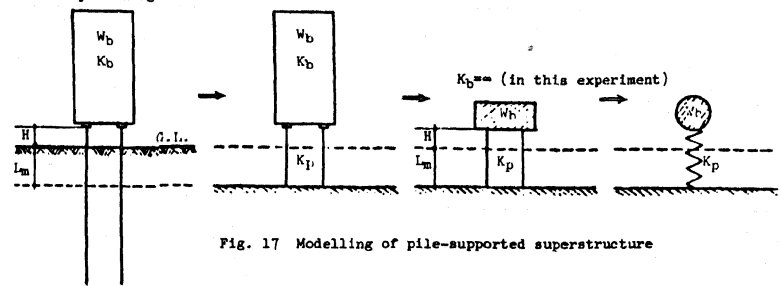
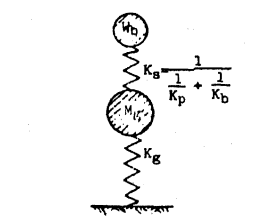


Fig. 17 Modelling of pile-supported superstructure



Two-degree of freedom system, composed of the models shown in Figs. 17 and 18.

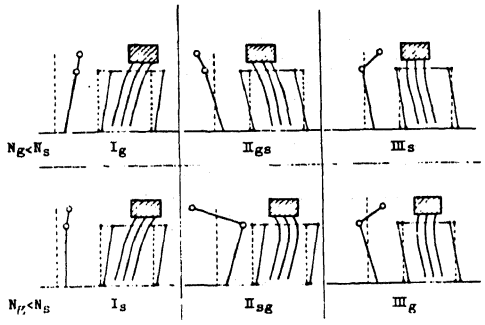


Fig. 19 Scheme of observed and computed modes