

Evaluation of site effects: development of the semiquantitative abacuses in Lazio Region (Italy)

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SUMMARY:

In this paper the procedure for the development of the regional abacuses (level 2), as prescribed in the Italian Guidelines for the Seismic Microzonation, is presented. These abacuses are finalized to obtain the values of the expected amplification, due to the presence of the deposits on bedrock. During the project the following steps have been performed: choice of the seismic inputs, choice of the numerical code, choice of the structure of the abacuses, analyses of the collected data, numerical analyses and construction of the abacuses. Therefore 5 abacuses, concerning to 5 geologic groups have been pointed out. The abacuses are constructed by table considering two inputs: the equivalent average velocity and the depth of the bedrock, the amplification is expressed in term of the FH value, calculated considering the elastic acceleration response spectra, as a ratio between the integral of output and input calculated in the period range between 0.1-0.5s.

Keywords:

Abacuses, Microzonation, Numerical analyses, Amplification factor, Lazio Region.

1. INTRODUCTION

The Italian Guidelines for the Seismic Microzonation (ICMS) (GdL MS, 2008) prescribe 3 levels for the microzonation studies: the Level 1 (L1) (qualitative approach) is dedicated to the individuation of the areas that can produce amplification and/or instability phenomena. The Level 2 (L2) (semiquantitative approach) consists in the definition of the expected amplification factors through the application of abacuses, that starting from the individuation of the thickness of the deposits (z) and the equivalent average velocity of the shear waves (V_{SH}), gives the level of the expected amplification. The Level 3 (L3) (quantitative approach) prescribes an evaluation of the quantitative level of the amplification and instability through the application of numerical and experimental analyses. In Region Lazio codes (DGR 545/2010), the L1 must be performed for all municipality territory to define the seismic stable areas, the seismic amplification areas and the instable one's. The L2 studies will be carry out in the amplification and instable areas only, like defined by L1, while the L3 where the L2 shows an high level of amplification and for the Strategic and Relevant Structures for Civil Protection (barracks, schools, university and so on – DGR 387/09). So, the aim of the paper has been the point out of the regional abacuses, in the Lazio Region, for L2 studies, as prescribed in the ICMS. The requirement to have regional abacuses derived by the consideration that the ICMS abacuses is devoted to a general application for the entire Italian territory, so the specific regional geologic situations aren't sufficiently represented. Moreover, in Lazio Region, the recent regional codes, for the planning and the mitigation of seismic risk, prescribe the use of specific regional abacuses (DGR 490/2011).

The structure of the developed regional abacuses is similar to the structure of the ICMS abacuses, but just in term of input parameters, whereas it is different in term of output parameter and of some validation criteria of the abacuses itself. The requirement to modify the output parameter is linked to the new revisions of ICMS (Colombi et al., 2011). The applied procedure, through numerical analyses, to obtain the abacuses, has been structured in the following steps:

- choice of the seismic inputs;
- choice of the numerical code;
- choice of the abacuses structure;

- analysis of the collected data;
- numerical analyses;
- construction of the abacuses;
- use of the abacuses.

2. CHOICE OF THE SEISMIC INPUTS

To define the accelerograms used in the numerical analyses, the new seismic zonation of Lazio Region (DGR 387/2009) and the study of the ENEA (2009) have been considered.

In this new seismic zonation, the regional territory has been divided in 5 seismic subzones (1, 2A, 2B, 3A, 3B), considering the expected horizontal acceleration value (a_{rif}), characterized by a return period of 475 years. Moreover the study has been pointed out the recorded accelerogram sets assigned to each “Unità Amministrativa Sismica” (UAS) that correspond to a Municipality or to areas of itself. Each set is characterized by 5 recorded accelerograms, modified in according to the expected response spectrum of each UAS, deriving from the seismic hazard analysis performed by the ENEA study.

To have a sufficient representativeness of the regional seismic hazard in term of accelerograms, 4 reference UAS have been chosen, in particular:

Vallerotonda: for the maximum value of the a_{rif} of the seismic subzone 1;

Monte San Giovanni Campano: for the minimum value of the a_{rif} of the seismic subzone 2A;

Roma Municipio V: for the minimum value of the a_{rif} of the seismic subzone 3A;

Ponza: for the minimum value of the a_{rif} of the seismic subzone 3B.

The numerical analyses have been performed using all the 4 selected accelerogram sets, calculating the average results into each set and between the sets. In the Figure 1, as an example, for the Roma V UAS, the 5 used accelerograms, each relative elastic acceleration response spectrum, the average spectrum of the 5 accelerograms and the Municipality code spectrum for the subsoil A, considering as bedrock, (NTC, 2008) are shown.

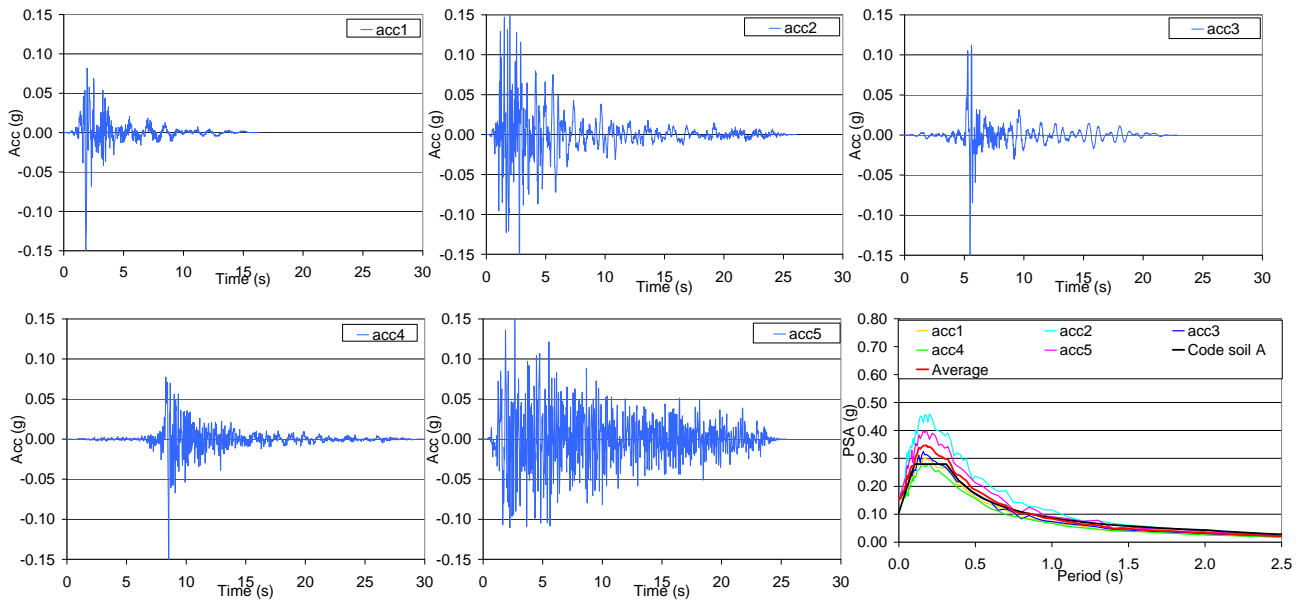


Figure 1. Accelerograms and response spectra for the Roma V UAS

3. CHOICE OF THE NUMERICAL CODE

Considering the objectives of this research, as the evaluation of the seismic amplification only due to geologic effects, a mono-dimensional numerical code has been chosen, finalized to compute the seismic response of horizontally layered soil deposits.

In the code the soil profile is idealized as a system of homogeneous, visco-elastic sub-layers of infinite

horizontal extent (Kelvin-Voigt). The response of this system is calculated considering vertically propagating shear waves: each layer is characterized by the thickness h , the density ρ , the initial shear modulus G_0 or the velocity of the shear waves V_s and the initial damping ratio D_0 . The bedrock is considered deformable, to avoid the energy of reflection waves into the model, in fact a rigid layer reflects all the reflected waves from the surface, instead in the case of the deformable layer, the waves are spread into the bedrock, so the code requires the bedrock parameters as the density ρ , the velocity of the shear waves V_s and the damping ratio D . The code adopts the equivalent linear analysis using an iterative procedure to obtain, in each iteration, the characteristics of the soil compatible with the effective strain in each layer. Therefore the process is iterative and the code works in the frequency domain, using the Fourier analysis.

4. CHOICE OF THE ABACUSES STRUCTURE

As described in the introduction, the structure of the proposed abacuses is similar to that reported in the ICMS, in term of input parameters, on the contrary it is different for the output parameter and for some validity criteria. The input parameters of the regional abacuses are: the thickness of the deposits z and their average equivalent velocity V_{SH} , calculated until the bedrock, using the following formula:

$$V_{SH} = z / \sum_{i=1}^n h_i / V_{Si}$$

where:

- V_{SH} = equivalent average velocity
- z = thickness of the deposits
- h_i = thickness of each layer of the deposits
- V_{Si} = shear wave velocity S of each layer of the deposits
- n = number of the layers

In the abacuses of L2, the values of the input parameters z and V_{SH} are divided by a range of 5-10 m for z and by a range of 50-100 m/s for V_{SH} , excluding the values of 180 m/s and 360 m/s, that have been chosen as prescribed in NTC (2008).

The output parameter is represented by the amplification factor FH , defined using the elastic acceleration response spectra (PSA), considering a critical damping (ξ) of 5%, as a ratio between the integrals of output and input calculated in the period range T of 0.1-0.5 s (Colombi et al., 2011).

One or more graphics V_s - z , delimiting the validity area for the abacus application, are associated to each abacus.

5. ANALYSIS OF THE COLLECTED DATA

To perform the numerical analyses it is necessary to know, for each geophysical unit, the value of the thickness h , the density ρ , the velocity of the shear waves V_s , the initial damping ratio D_0 and the relative decay curves of the normalized shear modulus G/G_0 and the damping ratio D with the shear strain γ . An amount of 42 geophysical investigations (Down-Hole and MASW) have been collected, to have information on the thickness and velocity V_s . The different behaviours of the velocity V_s correlating to the depth z are represented in Figure 2. As shown in Figure 2 the variability of the behaviour V_s - z is sufficiently large and able to consider these data as statistically suitable.

Each behaviour is associated to a specific geologic contest and particularly the data have been subdivided in 5 different units:

- alluvial ad debris gravels: n. 8 investigations;
- weathering sands (sandstone – travertine and tuff): n. 8 investigations;
- pyroclastic deposits: n. 7 investigations;
- alluvial sands: n. 6 investigations;
- clays and silts: n. 13 investigations.

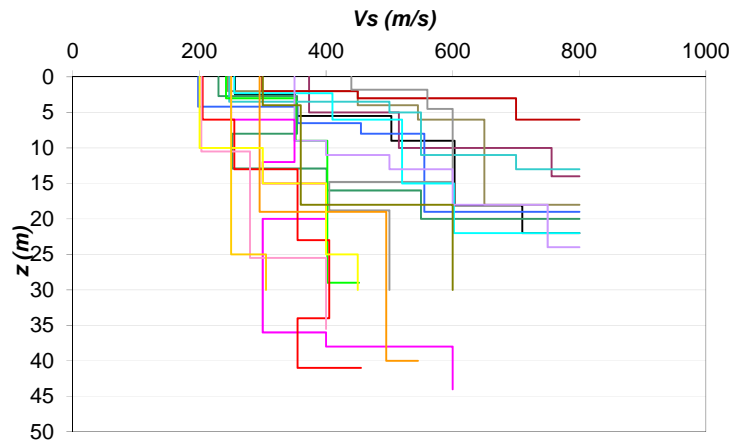


Figure 2. Behaviour of the collected V_s - z

The different units have been grouped on the basis of similar behaviour of V_s - z in 6 groups:

- alluvial gravels, debris gravels and weathering sands (sandstone – travertine and tuff);
- 3 groups for the alluvial sands and pyroclastic deposits;
- 2 groups for the clays and silts.

For each group one or more velocity gradients have been associated, that defines the field in which the experimental data are present:

- alluvial gravels, debris gravels and weathering sands (sandstone – travertine and tuff) characterized by a unique velocity gradient, reported in Figure 3;
- alluvial sands and pyroclastic deposits characterized by 3 velocity gradients, reported in Figure 4;
- clays and silts characterized by 2 velocity gradients, reported in Figure 5.

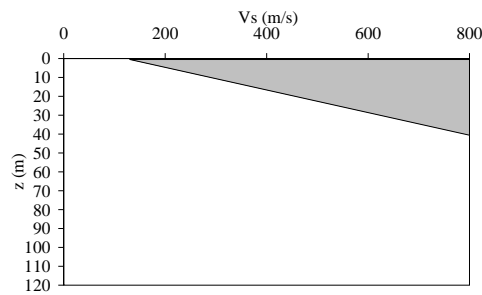


Figure 3. Boundary field of experimental data for the alluvial and debris gravels and weathering sands (in grey)

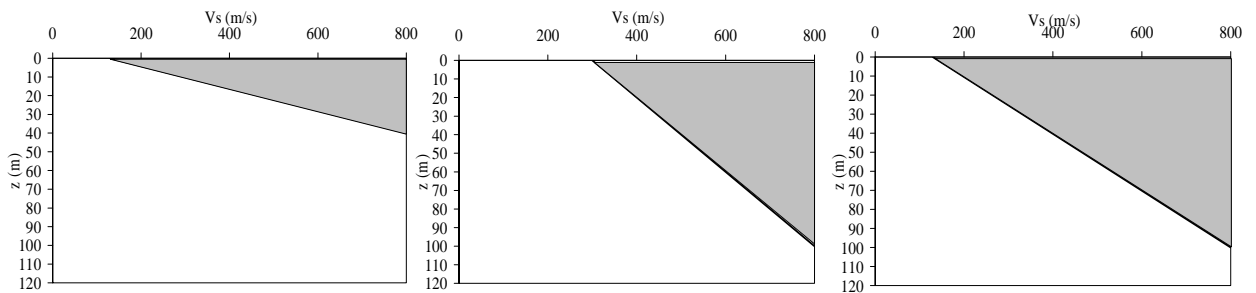


Figure 4. Boundary field of experimental data for the alluvial sands and pyroclastic deposits (in grey)

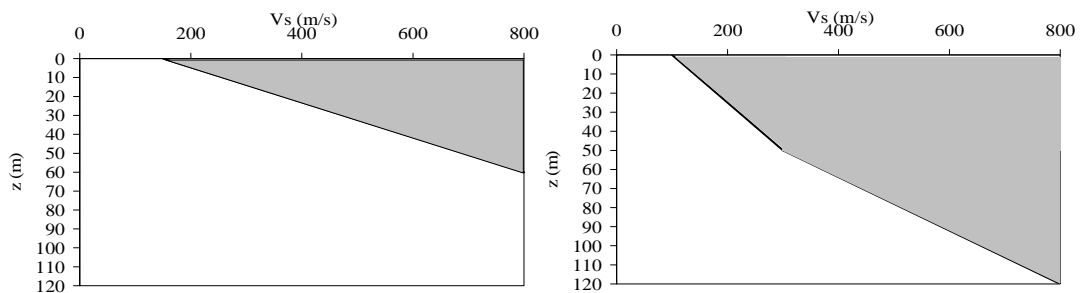


Figure 5. Boundary field of experimental data for the clays and silts (in grey)

The values of the initial damping ratio (D_0) of each group and the relative decay curves (G/G_0 and D correlating with γ) have been selected by bibliographic data, chosen into the available rich database, on the basis of geologic and geotechnical similarity.

In particular, for each group the following decay curves have been applied (Figure 6):

- alluvial ad debris gravels: Rollins (1998);
- weathering sands and pyroclastic deposits: Pergalani et al. (1999);
- alluvial sands: Seed & Idriss (1970);
- clays and silts: Working Group MS-AQ (2010).

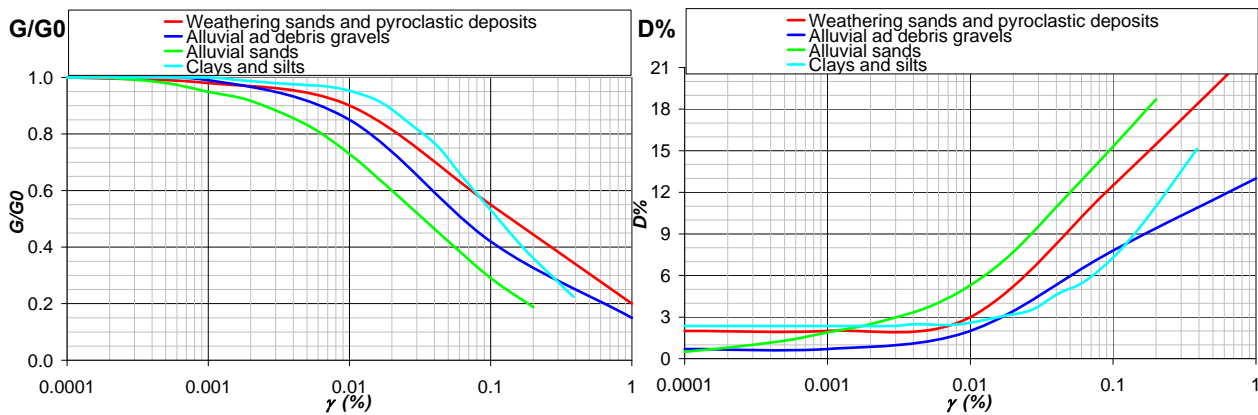


Figure 6. Decay curves for each examined group

Due to the lack of direct data, for the values of the density of each group, an increasing value, correlating to the depth z and to the V_s values, has been considered; in particular:

- 1.7 and 1.8 g/cm^3 in the interval of V_s between 200 and 300 m/s
- 1.8 and 1.9 g/cm^3 in the interval of V_s between 300 and 500 m/s
- 1.9 and 2.0 g/cm^3 in the interval of V_s between 500 and 600 m/s
- 2.0 and 2.1 g/cm^3 in the interval of V_s between 600 and 700 m/s
- 2.2 g/cm^3 for V_s 800 m/s.

6. NUMERICAL ANALYSES

On the basis of the collected data, the numerical analyses have been performed, using the selected numerical code and applying in each geophysical column the 4 sets of accelerograms, characterized by 5 accelerograms each one.

For each individuated velocity gradient, the geophysical columns, correlated to the available geophysical investigation (DH and MASW), have been analyzed; then an amount of geophysical columns, varying the thickness h and the velocity V_s into the validity area, have been constructed and analyzed. Each analyzed geophysical column has been defined in term of the couple V_{sH-Z} and the results of the analyses are expressed in term of amplification factor FH , calculated as average between the FH derived by the application of the 5 accelerograms of each set and than as average between the FH of the 4 sets.

The results show a negligible difference between the application of the more energetic sets of accelerograms (Vallerotonda e Monte San Giovanni Campano) and the lesser ones (Roma V e Ponza); therefore it was possible to analyzed these results into an unique database, to obtain abacus of L_2 independent of the level of the seismic hazard and applicable in all the regional territory. The analyses show an expected shear strain level γ into the range 0.01-0.05%, which can be considered relatively low, compatible to the used numerical code.

7. CONSTRUCTION OF THE ABACUSES

The choice to have the regional abacuses similar to the abacuses of ICMS has prescribed the use of

only two input parameters (V_{SH} and z).

The analyses have been shown that the same couple V_{SH-z} values can be generated by different combination of thickness h and velocity V_s of the geophysical unit, and consequently, to the same couple V_{SH-z} , different values of FH are associated. To obtain a correlation considering only two parameters as the FH value (output parameter of the abacus) and the couple V_{SH-z} values (input parameters of the abacus), the parameter T (dominant period of the geophysical column) has been introduced, so defined:

$$T = 4 \sum_{i=1}^n h_i / \left(\sum_{i=1}^n V_{Si} h_i / \sum_{i=1}^n h_i \right)$$

where:

- T = dominant period of the column
- h_i = thickness of the geophysical unit
- V_{Si} = velocity of the geophysical unit

Each analyzed geophysical column has been described by the relative couple V_{SH-z} , the relative T and the relative FH.

Different correlations of FH-T, using polynomial functions of 2° and 3° order, have been individuated and to each correlation (FH-T) some different couple V_{SH-z} have been associated.

So each abacus has been constructed using the FH values obtained by the correlation curves FH-T in the correspondent table V_{SH-z} , characterized by a specific T value.

In the Figures 7, 8, 9, 10 and 11, for each group, the correlation curves FH-T and the relative associations in the table of the abacus are reported. In the Figures the table fields in grey correspond to the not applicable area of abacus.

In the Figures 12, 13, 14, 15 and 16 the abacuses, related to the 5 groups characterized by different velocity gradient and suitable for the entire regional territory, are presented. The abacuses are formed by tables considering two inputs (V_{SH} and z), one output (FH) and graphics of validity areas.

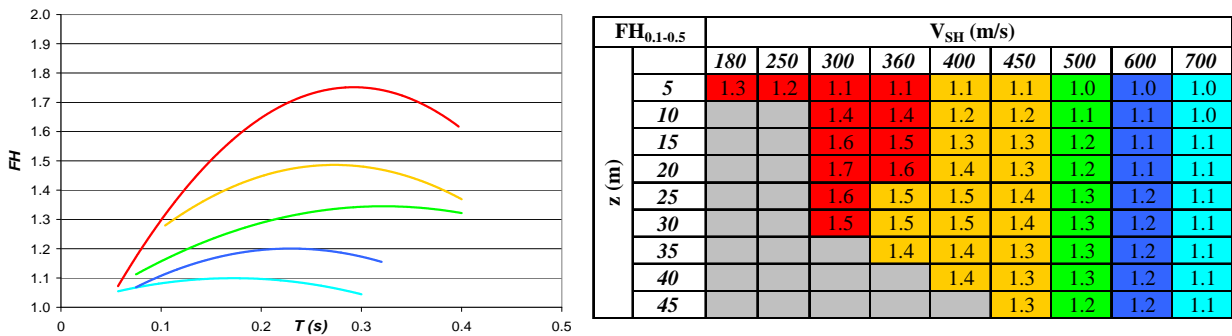


Figure 7. Association between the FH-T and the relative fields V_{SH-z} of the abacus for the alluvial and debris gravels and weathering sands

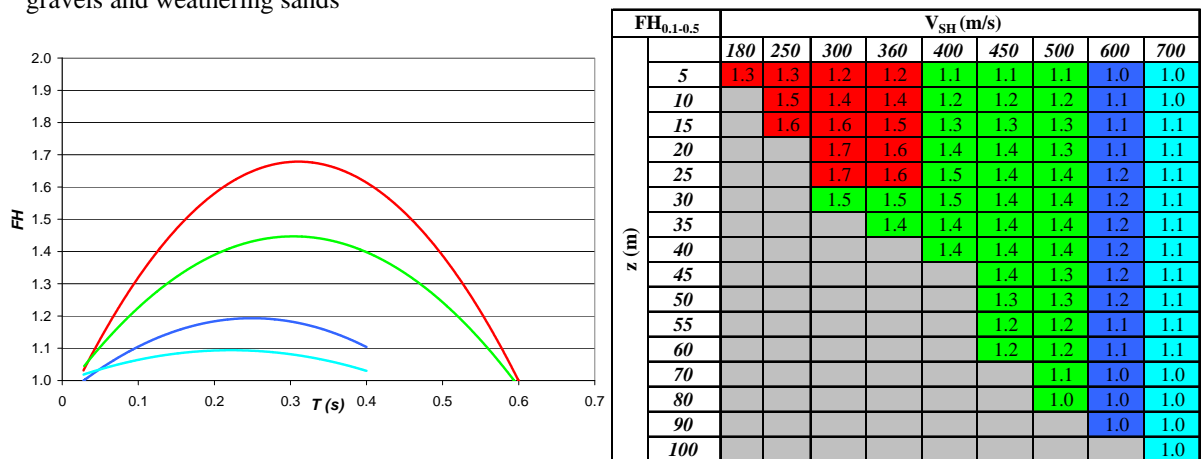


Figure 8. Association between the FH-T curves and the relative fields V_{SH-z} of the abacus for the alluvial sands and pyroclastic deposits characterized by minimum velocity gradient

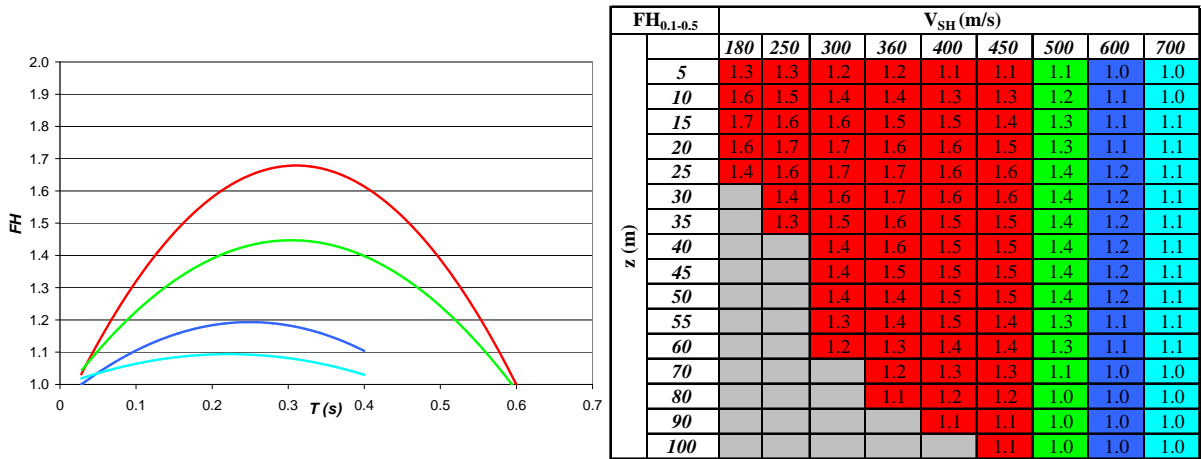


Figure 9. Association between the FH-T curves and the relative fields V_{SH-z} of the abacus for the alluvial sands and pyroclastic deposits characterized by maximum velocity gradient

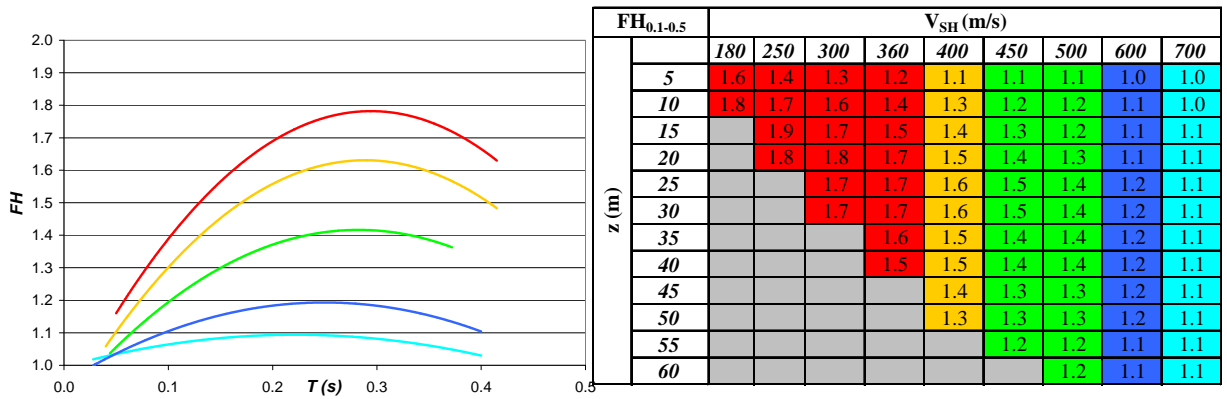


Figure 10. Association between the FH-T curves and the relative fields V_{SH-z} of the abacus for the clays and silts characterized by minimum velocity gradient

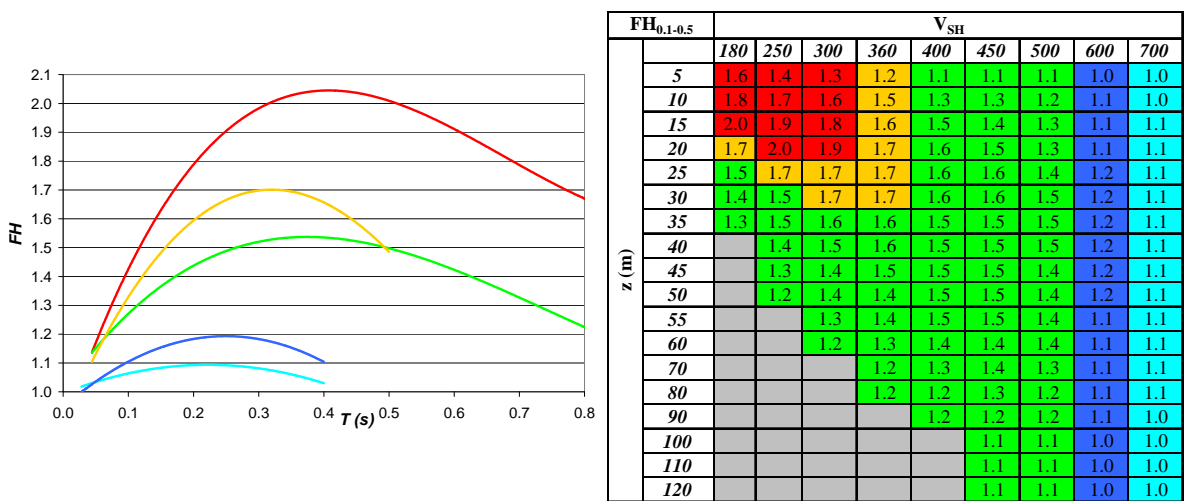


Figure 11. Association between the FH-T curves and the relative fields V_{SH-z} of the abacus for the clays and silts characterized by maximum velocity gradient

FH _{0.1-0.5}		V _{SH} (m/s)								
		180	250	300	360	400	450	500	600	700
z (m)	5	1.3	1.2	1.1	1.1	1.1	1.1	1.0	1.0	1.0
	10			1.4	1.4	1.2	1.2	1.1	1.1	1.0
	15			1.6	1.5	1.3	1.3	1.2	1.1	1.1
	20			1.7	1.6	1.4	1.3	1.2	1.1	1.1
	25			1.6	1.5	1.5	1.4	1.3	1.2	1.1
	30			1.5	1.5	1.5	1.4	1.3	1.2	1.1
	35				1.4	1.4	1.3	1.3	1.2	1.1
	40					1.4	1.3	1.3	1.2	1.1
	45						1.3	1.2	1.2	1.1

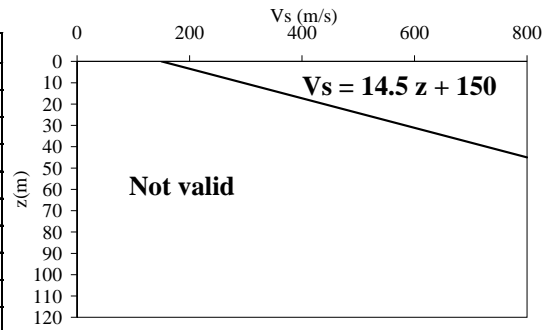


Figure 12. Abacus for the alluvial and debris gravels and weathering sands

FH _{0.1-0.5}		V _{SH} (m/s)								
		180	250	300	360	400	450	500	600	700
z (m)	5	1.3	1.3	1.2	1.2	1.1	1.1	1.1	1.0	1.0
	10		1.5	1.4	1.4	1.2	1.2	1.2	1.1	1.0
	15		1.6	1.6	1.5	1.3	1.3	1.3	1.1	1.1
	20			1.7	1.6	1.4	1.4	1.3	1.1	1.1
	25			1.7	1.6	1.5	1.4	1.4	1.2	1.1
	30			1.5	1.5	1.5	1.4	1.4	1.2	1.1
	35				1.4	1.4	1.4	1.4	1.2	1.1
	40					1.4	1.4	1.4	1.2	1.1
	45						1.4	1.3	1.2	1.1
	50						1.3	1.3	1.2	1.1
	55						1.2	1.2	1.1	1.1
	60						1.2	1.2	1.1	1.1
	70							1.1	1.0	1.0
	80							1.0	1.0	1.0
	90								1.0	1.0
	100									1.0

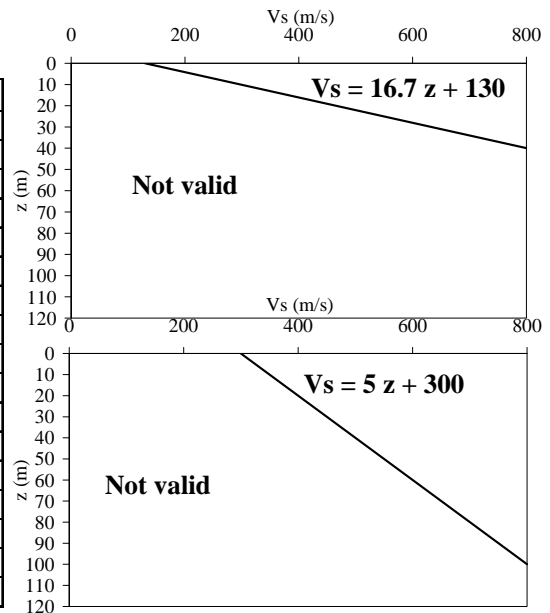


Figure 13. Abacus for the alluvial sands and pyroclastic deposits characterized by minimum velocity gradient

FH _{0.1-0.5}		V _{SH} (m/s)								
		180	250	300	360	400	450	500	600	700
z (m)	5	1.3	1.3	1.2	1.2	1.1	1.1	1.1	1.0	1.0
	10	1.6	1.5	1.4	1.4	1.3	1.3	1.2	1.1	1.0
	15	1.7	1.6	1.6	1.5	1.5	1.4	1.3	1.1	1.1
	20	1.6	1.7	1.7	1.6	1.6	1.5	1.3	1.1	1.1
	25	1.4	1.6	1.7	1.7	1.6	1.6	1.4	1.2	1.1
	30		1.4	1.6	1.7	1.6	1.6	1.4	1.2	1.1
	35		1.3	1.5	1.6	1.5	1.5	1.4	1.2	1.1
	40			1.4	1.6	1.5	1.5	1.4	1.2	1.1
	45			1.4	1.5	1.5	1.5	1.4	1.2	1.1
	50			1.4	1.4	1.5	1.5	1.4	1.2	1.1
	55			1.3	1.4	1.5	1.4	1.3	1.1	1.1
	60			1.2	1.3	1.4	1.4	1.3	1.1	1.1
	70				1.2	1.3	1.3	1.1	1.0	1.0
	80				1.1	1.2	1.2	1.0	1.0	1.0
	90					1.1	1.1	1.0	1.0	1.0
	100						1.1	1.0	1.0	1.0

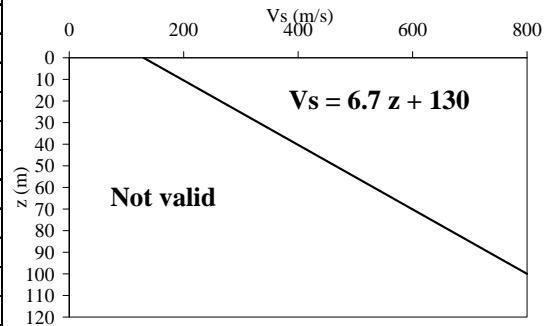


Figure 14. Abacus for the alluvial sands and pyroclastic deposits characterized by maximum velocity gradient

FH _{0.1-0.5}		V _{SH} (m/s)								
		180	250	300	360	400	450	500	600	700
z (m)	5	1.6	1.4	1.3	1.2	1.1	1.1	1.1	1.0	1.0
	10	1.8	1.7	1.6	1.4	1.3	1.2	1.2	1.1	1.0
	15		1.9	1.7	1.5	1.4	1.3	1.2	1.1	1.1
	20		1.8	1.8	1.7	1.5	1.4	1.3	1.1	1.1
	25			1.7	1.7	1.6	1.5	1.4	1.2	1.1
	30			1.7	1.7	1.6	1.5	1.4	1.2	1.1
	35				1.6	1.5	1.4	1.4	1.2	1.1
	40				1.5	1.5	1.4	1.4	1.2	1.1
	45					1.4	1.3	1.3	1.2	1.1
	50					1.3	1.3	1.3	1.2	1.1
	55						1.2	1.2	1.1	1.1
	60							1.2	1.1	1.1

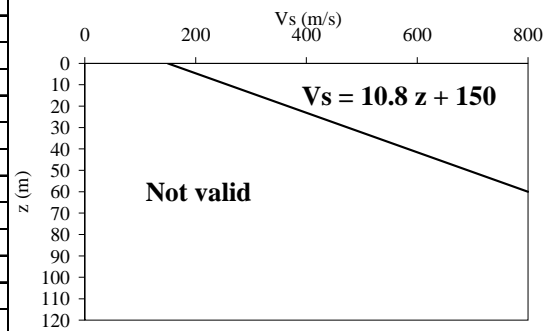


Figure 15. Abacus for the clays and silts characterized by minimum velocity gradient

FH _{0.1-0.5}		V _{SH}								
		180	250	300	360	400	450	500	600	700
z (m)	5	1.6	1.4	1.3	1.2	1.1	1.1	1.1	1.0	1.0
	10	1.8	1.7	1.6	1.5	1.3	1.3	1.2	1.1	1.0
	15	2.0	1.9	1.8	1.6	1.5	1.4	1.3	1.1	1.1
	20	1.7	2.0	1.9	1.7	1.6	1.5	1.3	1.1	1.1
	25	1.5	1.7	1.7	1.7	1.6	1.6	1.4	1.2	1.1
	30	1.4	1.5	1.7	1.7	1.6	1.6	1.5	1.2	1.1
	35	1.3	1.5	1.6	1.6	1.5	1.5	1.5	1.2	1.1
	40		1.4	1.5	1.6	1.5	1.5	1.5	1.2	1.1
	45		1.3	1.4	1.5	1.5	1.5	1.4	1.2	1.1
	50		1.2	1.4	1.4	1.5	1.5	1.4	1.2	1.1
	55			1.3	1.4	1.5	1.5	1.4	1.1	1.1
	60			1.2	1.3	1.4	1.4	1.4	1.1	1.1
70				1.2	1.3	1.4	1.3	1.1	1.1	
80				1.2	1.2	1.3	1.2	1.1	1.1	
90					1.2	1.2	1.2	1.1	1.0	
100						1.1	1.1	1.0	1.0	
110						1.1	1.1	1.0	1.0	
120						1.1	1.1	1.0	1.0	

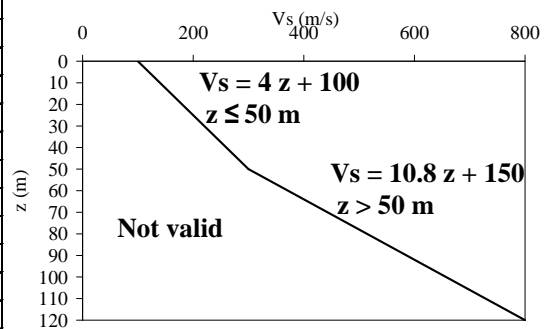


Figure 16. Abacus for the clays and silts characterized by maximum velocity gradient

9. USE OF THE ABACUSES

As mentioned, the regional territory has been subdivided in UAS, that correspond to a Municipality or a part of itself, particularly if the Municipality is characterized by a large territory (Roma, Rieti, Pescorocchiano).

The use of the abacuses considers the values, for each UAS, of a thresholds S_s (Stratigraphic coefficient) derived by the national seismic hazard and by the elastic acceleration response spectra prescribed by the national code (NTC, 2008). In particular the national code considers 4 types of soils that can produce amplification phenomena (B-C-D-E soils) and a bedrock (A soil), for each soil the national code gives an acceleration response spectrum, relating to different points of seismic hazard.

So 4 different threshold values S_s, for each UAS, have been calculated as a ratio, considering the acceleration response spectra, between the integral of the output (B-C-D-E soils) and of the input (A soil) in the period range of 0.1-0.5 s.

The comparison between the S_s value and FH value, obtained by the abacuses, permits to distinguish the areas where it is necessary to perform seismic analyses of L3 of the ICMS, as described in the integration of ICMS (Colombi et al., 2011), and prescribed in the regional codes, when the FH > S_s + 0,1, from the areas where it is possible to apply the acceleration response spectra derived by the national code.

10. CONCLUSION

The aim of the project has been the development of regional abacuses, finalized to the evaluation of the expected amplifications, using a semiquantitative approach (L2), as prescribed by the ICMS. The requirement to have regional abacuses derived by the consideration that the ICMS abacuses are devoted to a general application for the entire Italian territory, so the specific regional geologic situations aren't sufficiently represented. Moreover, in Lazio Region, the recent regional codes, for the planning and the mitigation of seismic risk, prescribe the use of specific regional abacuses.

During the project the following steps have been performed: choice of the seismic inputs, choice of the numerical code, choice of the structure of the abacuses, analyses of the collected data, numerical analyses and construction of the abacuses.

The application of the abacuses, defining the value of the expected amplification FH, allows, in urban planning phase, to:

- perform a list of areas, characterized by different hazards due to different values of expected amplifications;
- define the suitability of the investigated areas, during the planning phase (DGR 2649/99);
- define the areas where it is necessary to apply the L3 of ICMS, because the FH values is higher than the Ss threshold, derived by the national code, to obtain more adequate acceleration response spectra.

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