

# FLEXURAL PERFORMANCE ON RC AND PRECAST CONCRETE COLUMNS WITH ULTRA HIGH STRENGTH MATERIALS UNDER VARYING AXIAL LOAD

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## **ABSTRACT :**

In this experimental study, it was clarified the structural performance of reinforced concrete (RC) and precast concrete (PCa) columns with ultra-high-strength materials. Anti-symmetrical cyclic lateral loads and varying axial loads corresponding to the axial load acting on the exterior column in lower story were applied to the column specimens. The alternative of the design standard strength ( $F_c$ ) of the concrete is 80 MPa and 120 MPa, and the nominal yield strength of the main reinforcing bar is 490 MPa and 685 MPa. The nominal yield strength of shear reinforcement in a column is 1275 MPa. The six column specimens were manufactured with the combinations of such materials.

The flexural capacity obtained from the experiment was evaluated using the equation of Building Code and Commentary ACI 318-02(2002), and it was found that the equation overestimated the flexural capacity for the  $F_c$  120 MPa specimen. Therefore, the flexural capacity of each specimen was reevaluated using rectangular stress blocks designed for high-strength concrete.

**KEYWORDS:** ultra-high-strength material, reinforced concrete column, precast concrete column, varying axial load, flexural performance, evaluation of capacity.

# **1. INTRODUCTION**

In recent years, RC buildings are becoming super-high-rise and long-span structures. In such buildings, the columns of the lower stories are subjected to large long-term axial loads. Moreover, when an earthquake occurs, a large varying axial load acts on the exterior columns. Therefore, it is necessary to use higher strength concrete and reinforcing bars, and also the use of more PCa members to rationalize the construction of such super-high-rise buildings in shorter work periods is inevitable.

Six specimens which consist of RC and PCa columns, were manufactured by combining concrete design nominal strength ( $F_c$ ) 80 MPa and 120 MPa, nominal yield strength of the longitudinal reinforcements 490 MPa (SD490) and 685 MPa (USD685), and nominal yield strength of shear reinforcement 1275 MPa (SBPD1275). This study aimed to clarify the flexural performance of column members made of ultra-high-strength materials by conducting a static bending shear force test on specimens of external columns in the lower stories subjected to varying axial load.

Furthermore, the flexural capacity obtained from the experiment was evaluated to determine whether or not the rectangular stress block method in accordance with the equation of Building Code and Commentary ACI 318-02 (2002), which was designed for normal-strength concrete, is applicable to high-strength concrete such as the specimens used in this study.

### 2. EXPERIMENTAL PROGRAM

#### 2.1. Description of Specimens

Table 2.1 shows the structural specifications of each specimen. The six specimens have an area of 330 (width:

# The 14<sup>th</sup> World Conference on Earthquake Engineering October 12-17, 2008, Beijing, China



b) x 330 (overall depth: D) (mm) which is equivalent to 1/3 of the actual column cross-sectional area and a shear span ratio  $(M/(V \cdot D))$  of 2.0 in consideration of flexural failure. As shown in Table 2.1, the specimens are roughly divided into three specimens of  $F_c$  80 MPa and another three specimens of  $F_c$  120 MPa. The values of longitudinal reinforcements 16-D22(# 7) (Grade: SD490) and 16-D19(# 6) (Grade: USD685) for monolithic cast RC column members with respect to each  $F_c$  value, and full-PCa column members of the latter value of 16-D19 (USD685) were taken into consideration as the variable factors of the specimens. Four of the 16 longitudinal reinforcements are core reinforcing bars for use in exterior columns in the lower stories. The lateral ties (hoops), used commonly in all the specimens, were small-diameter deformed PC steel bars arranged in a single-stroke enclosed lattice pattern.

The specimens 'C80D22' and 'C80D19' shown in Table 2.1 have different ratios of total area of longitudinal reinforcements to the gross area of column concrete cross-section  $(A_{st}/A_g)$  but their calculated flexural strengths are almost the same. On the other hand, the specimen 'PC80D19' uses a mortar-filled splice sleeve joint to join the longitudinal reinforcements in both column base and capital. The hoops used in these joint sections are the same as those used in other sections. The specimens 'C120D22', 'C120D19' and 'PC120D19' have the same structural specifications as the specimens 'C80D22', 'C80D19', and 'PC80D19' respectively, except for their  $F_c$  being 120 MPa. Figure 2.1 shows the shapes of specimens and their bar arrangement.

Table 2.2 shows the mechanical properties of the reinforcements used in this experiment. Table 2.3 shows the mechanical properties of the concrete. The concrete materials for the specimens include high-early-strength Portland cement for  $F_c$  80 MPa and normal Portland cement for  $F_c$  120 MPa with about 10 WT% of silica fume as admixture. Crushed stones having the maximum diameter of 13 mm were used as coarse aggregate for all.

Table 2.1         Structural specifications of test specimens.									
	Longitudinal	Concrete	Ноор	Varying					
Specimen	reinforcement	F <sub>c</sub>	(PC steel bar)	axial load					
	$A_{st}/A_g(\%)$	(MPa)	р <sub>h</sub> (%)	Р					
C80D22	16-D22(SD490) 5.69%			Compressive:					
C80D19	16-D19(USD685)	F <sub>c</sub> 80		+0.55 <i>F</i> <sub>c</sub> bD					
PC80D19				$(+0.50F_{c}bD)^{*}$					
C120D22	16-D22(SD490) 5.69%	F 100	4-RB6.2 @50(SBPD	Tensile:					
C120D19	16-D19(USD685)	<i>F</i> <sub>c</sub> 120	1275/1420)	$-0.7A_{st}f_y$					
PC120D19	4.22%		0.73%						

\*0.50 $F_c bD$  in the case of  $F_c$  120 MPa. b (width)=330mm D (overall depth)=330mm h (clear height)=1320mm M/(VD) (shear span ratio)=2.0

Table 2.2	Mechanical	properties of reinforcements.
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	fy	εγ	$f_t$	Es	Elongation	*Taken as the 0.2% proof stre
Bar size	MPa		MPa	GPa	%	$f_y$ = yield strength
D22(#7)(SD490)	522	0.0028	715	196	17	$\varepsilon_y$ = yield strain
D19(#6)(USD685)	745	0.0057	1008	202	12	$f_t$ = tensile strength
Hoop: RB6.2(#2)	1275*	0.0077	1442	198	7	$E_s$ = elastic modulus
(SBPD1275/1420)		0.0011		100	•	

Table 2.3 Me	chanical prop	erties of concre	ete and mortar.
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	f <sub>c</sub> ′	E <sub>c</sub>	$_{c}f_{t}$		f <sub>c</sub> ′	E <sub>c</sub>	$_{c}f_{t}$
Specimen	MPa	GPa	MPa	Specimen	MPa	GPa	MPa
C80D22	92.4	37.4	5.95	C120D22	135.6	44.3	7.44
C80D19	98.4	38.7	5.48	C120D19	136.0	44.3	6.91
PC80D19	98.7	39.4	5.00	PC120D19	134.4	44.3	6.80
J. mortar*	136.6	41.4	—	J. mortar*	147.8	43.6	

\*Joint mortar and grout.

- $f_c$ ' =concrete cylinder
- compressive strength
- $E_c$  =elastic modulus
- $_{c}f_{t}$  =splitting strength



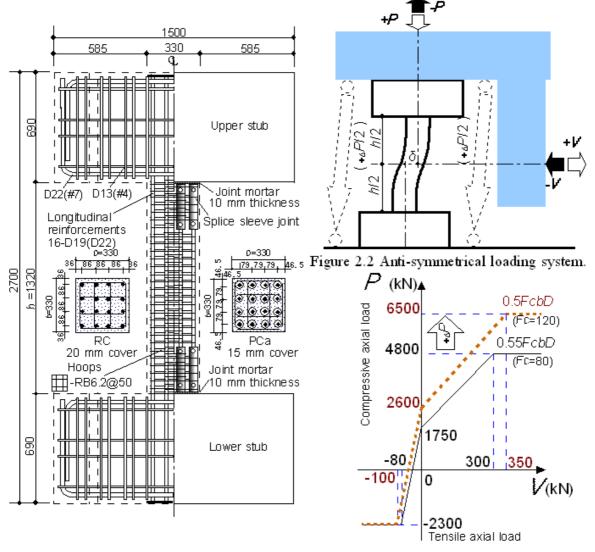


Figure 2.1 Dimensions of specimens. (All dimensions in mm)

Figure 2.3 Loading method of varying axial load.

# 2.2. Test Setup and Loading Sequence

For loading specimens, an L-shaped loading beam as shown in Figure 2.2 was used. While varying axial load was applied to the specimen, anti-symmetric static bending shear force, with the center level of the clear height being the point of contraflexure, was also applied to the specimen repeatedly, with positive and negative horizontal shear forces applied alternately.

Figure 2.3 shows the loading method of varying axial load, where the compressive axial load is expressed as positive load. First, long-term compressive axial load of  $0.2F_cbD$  was applied. Then, axial load (P) was gradually changed in accordance with the horizontal shear force (V). The upper limit and lower limit of the axial load were the compressive axial load  $0.55F_cbD$   $(0.50F_cbD)$  in the case of  $F_c$  120 MPa) in positive shear force loading and the tensile axial load  $-0.7A_{st} f_y$  ( $A_{st} f_y$ : product of the total area of the longitudinal reinforcements and the actual yield strength) in negative shear force loading. The axial load was kept constant thereafter.

The horizontal shear force was controlled on the basis of story drift angle ( $R = \delta / h$ ,  $\delta$ :relative horizontal displacement between upper and lower stubs, *h*:clear height of column). The experiment was terminated after applying shear force once at  $R = \pm 2.5/1000$ , twice at  $R = \pm 5/1000$ ,  $\pm 10/1000$ ,  $\pm 15/1000$ , and  $\pm 20/1000$ , and once at  $R = \pm 30/1000$  and  $\pm 50/1000$  respectively.



### **3. DISCUSSION OF TEST RESULTS**

#### 3.1. Outline of the Results

Figure 3.1 shows the relationship between the shear force (V) and story drift angle (R) of all specimens with  $P-\Delta$  effect taken into consideration. The single-dot chained lines in the Figure 3.1 represent the proof strength in the case where the hysteretic curve with  $P-\Delta$  effect taken into consideration is lowered to a level that is 95% of the maximum shear force. Table 3.1 shows the shear strength and story drift angle of each loading. The shear strength values in the Table 3.1 are those with  $P-\Delta$  effect taken into consideration, except for the "first cracking".

Photo 3.1 shows the final conditions (R = +50/1000) of the specimens. The failure patterns shown in Photo 3.1 show flexural crushing in the column capital and column base of the specimens. With the PCa column specimens 'PC80D19' and 'PC120D19', the degree of shear cracking in the central area of the test section and crushing from the joints to the positions just above the joints was remarkable. However, no such phenomena as buckled longitudinal reinforcements and rupture of hoops were observed in any specimen.

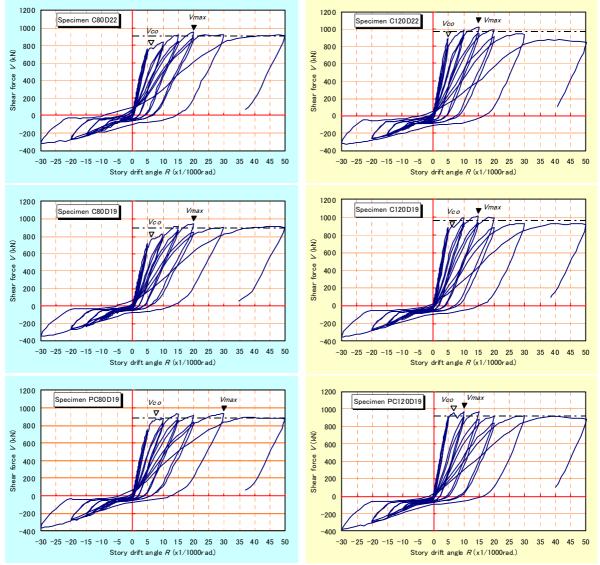


Figure 3.1 Relationship between the shear force (V) and story drift angle (R).



	Tuble 5.1 Experimental results of specimens.											
Specimen	fc'	±	Vcr	Rcr	Vy	Ry	Vco	Rco	Vmax	Rmax	Vul	Rul
opecimen	MPa	<u> </u>	kN	x1/1000	kN	x1/1000	kN	x1/1000	kN	x1/1000	kN	x1/1000
C80D22	92.4	+	—	—	755.5	5.47	774.7	5.92	948.9	20.05	909.5	50.07
C80D22	92.4	-	-51.9	-0.73	-75.4	-4.58	—	—	-325.4	-30.02	-325.4	-30.02
C80D19	98.4	+	—	—	786.2	9.99	770.3	6.48	938.8	20.02	900.5	50.03
C00D 19	30.4	-	-37.9	-0.48	-159.3	-9.70	—	—	-347.4	-29.64	-347.4	-29.64
PC80D19	98.7	+	—	—	838.6	10.93	870.5	7.61	935.1	29.26	873.4	50.03
FC00D19	90.7	-	-37.9	-0.50	-148.0	-9.42	—	—	-360.9	-29.33	-360.9	-29.33
C120D22	135.6	+	—	—	877.0	4.78	888.0	5.00	1022.7	15.03	849.5	50.10
C120D22		-	-54.9	-0.58	-89.8	-5.02	—	—	-326.2	-28.37	-326.2	-28.37
C120D19	136.0	+	—	—	972.5	12.08	892.0	6.08	1013.4	15.01	912.1	50.05
C120D19	130.0	-	-56.9	-0.61	-188.2	-12.74	—	—	-353.2	-30.02	-353.2	-30.02
PC120D19	134.4	+	—	—	897.1	7.96	955.1	6.73	968.8	10.02	881.1	50.17
FC IZUD IS	134.4	-	-53.9	-0.45	-123.3	-7.60	—	—	-385.2	-30.04	-385.2	-30.04
fc'	=	con	icrete cy	linder co	mpressi	ve streng	gth					
Vcr (Rcr)	<i>Vcr</i> ( <i>Rcr</i> ) = shear strength (drift angle) at the first cracking											

= shear strength (drift angle) at the yield of longitudinal reinforcement

= shear strength (drift angle) at the spalling of cover concrete (1st peak)

Table 3.1 Experimental results of specimens.

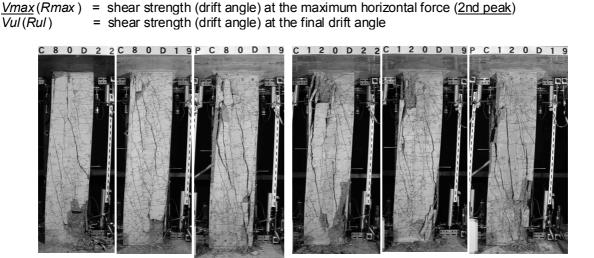


Photo 3.1 Final conditions (R = +50/1000) of specimens.

### 3.2. Strains in Axial Direction

Vy (Ry) Vco(Rco)

Figure 3.2 shows the relationship between the axial strain and story drift angle of each specimen. For the expression of the axial strains, the elongation displacement between upper and lower stubs at the axial position in the column was divided by the clear height of column (*h*) and the tensile strain was expressed as a positive value. The strain performance in the axial direction of the  $F_c$  80 MPa and  $F_c$  120 MPa specimens while applying tensile axial load remained almost the same. The axial strains of the  $F_c$  120 MPa specimen during the large deformation period at and after R = +10/1000 in compressive axial load application mode became large. Also from the appearance of final condition shown in Photo 3.1, it is clear that the degree of crushing in the  $F_c$  120 MPa specimen is larger than that in the  $F_c$  80 MPa specimen, together with spalling of cover concrete over a larger surface area of the  $F_c$  120 MPa specimen.

According to the equation of Building Code and Commentary ACI 318-02 (2002), the axial compressive capacity of a column member using normal-strength concrete is given by the following Eqn. 3.1.

$$P_0 = 0.85 f_c' (A_g - A_{st}) + A_{st} f_y$$
(3.1)

In connection with Eqn. 3.1 above, Ozbakkaloglu and Saatcioglu (2004) proposed the following equation as an axial compressive capacity expression applicable to a column using concrete of strengths from normal to high-strength level (120 MPa).

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$$P_{0 (\text{HSC})} = 0.9 \, k_4 \, f_c' (A_g - A_{st}) + A_{st} f_y \tag{3.2}$$

$$\kappa_4 = \gamma + (1 - \gamma) A_c / A_g \le 0.95$$

$$\gamma = 1.1 - 0.007 f_c' \le 0.8$$
(3.4)

$$\gamma = 1.1 - 0.007 J_c \le 0.8$$
 (3.2)

Table 3.2 shows the axial compressive capacity of each specimen obtained by using Eqns. 3.1 and 3.2. The rate of loaded axial force, which is obtained by dividing the compressive axial load (P) applied to each specimen by the product of the compressive strength of concrete ( $f_c$ ) and total cross-sectional area of the column ( $A_g$ ), is slightly larger in the  $F_c$  80 MPa specimen than in the  $F_c$  120 MPa specimen. However, calculation of the ratios of axial compressive capacity ( $P_0$ ), based on Eqns. 3.1 and 3.2, to the loaded axial force (P) resulted in a clearly greater ratio for the  $F_c$  120 MPa specimen in Eqn. 3.2 than in Eq. 3.1 of ACI 318-02 (2002). It is safe to assume that this greater ratio caused the increase in the axial strains of the  $F_c$  120 MPa specimen during the large story drift angle. There was no difference in the axial strains between RC column specimens prepared by monolithic casting and PCa column specimens.

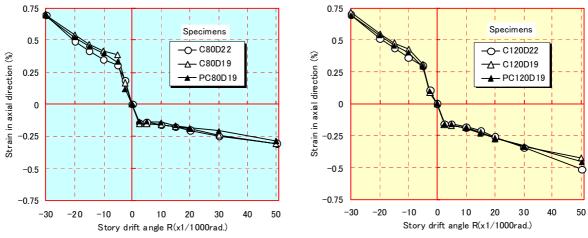


Figure 3.2 Relationship between the strain in the axial direction and story drift angle.

	Table 5.2 Axial compressive capacity of specificity.											
	fc'	Ag	Ac	Ast	Р	P/(fc'Ag)	$P_0$	$P/P_0$	mean	$P_{0(HSC)}$	P/P <sub>0(HSC)</sub>	mean
Specimen	MPa	mm <sup>2</sup>	mm <sup>2</sup>	$mm^2$	kN		kN			kN		
C80D22	92.4		80656	6192		0.477	11299	0.425		10562	0.454	
C80D19	98.4	108900	80656	4592	4800	0.448	12145	0.395	0.405	11248	0.427	0.442
PC80D19	98.7		71824	4592		0.447	12172	0.394		10823	0.444	
C120D22	135.6		80656	6192		0.440	15070	0.431		13006	0.500	
C120D19	136.0	108900	80656	4592	6500	0.439	15479	0.420	0.425	13367	0.486	0.503
PC120D19	134.4		71824	4592		0.444	15337	0.424		12426	0.523	
P =	P = unper limit of the compressive axial load											

 Table 3.2
 Axial compressive capacity of specimens

*P* = upper limit of the compressive axial load

 $P_0$  = nominal concentric compressive capacity, defined in Eqn. 3.1

 $P_{0(HSC)}$  = nominal concentric compressive capacity, defined in Eqn. 3.2

## 4. EVALUATION OF FLEXURAL CAPACITY

The experimental shear strength values for spalling of cover concrete and maximum shear force (referred to also as "first peak: *Vco*" and "second peak: *Vmax*") shown in Table 3.1 were compared with calculated values respectively, as shown in Table 4.1.

The calculated values, with respect to the coefficients ( $\alpha_1$  and  $\beta_1$ ) which constitute the rectangular stress block, were based on both (i) Equation of Building Code and Commentary ACI 318-02 (2002) and (ii) Equation proposed by Ozbakkaloglu and Saatcioglu (2004).



The coefficients  $\alpha_1$  and  $\beta_1$  represented by both (i) and (ii) at a compressive strength of concrete  $f_c' \ge 30$  MPa are shown below. The ultimate compressive strain at extreme fiber ( $\varepsilon_u$ ) is 0.003 in common.

(i) Equation of Building Code and Commentary ACI 318-02 (2002)

$$\alpha_1 = 0.85$$
 (4.1)

$$\beta_1 = 0.85 - 0.008 \left( f_c' - 30 \right) \ge 0.65 \tag{4.2}$$

(ii) Equation proposed by Ozbakkaloglu and Saatcioglu (2004)

$$\alpha_1 = 0.85 - 0.0014 (f_c' - 30) \ge 0.72$$

$$\beta_1 = 0.85 - 0.0020 (f_c' - 30) \ge 0.67$$
(4.3)
(4.4)

1000	Table 4.1 Comparison of experimental and calculated nexural capacity values.									
	<i>P-∆</i>	Vco	Vmax	$V_{ACI}$	1st	2nd	V <sub>HSC</sub>	1st	2nd	
Specimen	effect	kN	kN	kN	Vco/V <sub>ACI</sub>	Vmax/V <sub>ACI</sub>	kN	Vco/V <sub>HSC</sub>	Vmax/V <sub>HSC</sub>	
C80D22	no	746.3	853.1	726.8	1.03	1.17	727.4	1.03	1.17	
C00D22	yes	774.7	948.9	720.0	1.07	1.31	121.4	1.07	1.30	
C80D19	no	739.3	843.1	720.5	1.03	1.17	704 4	1.05	1.20	
CODIA	yes	770.3	938.8	720.5	1.07	1.30	704.4	1.09	1.33	
	no	834.1	857.1	697.2	1.20	1.23	680.6	1.23	1.26	
PC80D19	yes	870.5	935.1	097.2	1.25	1.34		1.28	1.37	
C120D22	no	855.3	924.8	000 0	0.88	0.95	050 0	1.00	1.08	
C120D22	yes	888.0	1022.7	968.6	0.92	1.06	858.8	1.03	1.19	
C120D19	no	852.4	929.6	930.5	0.92	1.00	819.6	1.04	1.13	
CIZUDI9	yes	892.0	1013.4	930.5	0.96	1.09	019.0	1.09	1.24	
PC120D19	no	911.1	903.7	896.9	1.02	1.01	788.2	1.16	1.15	
FC120D19	yes	955.1	968.8	090.9	1.06	1.08	100.2	1.21	1.23	
17 0		••					(0000)			

Table 4.1 Comparison of experimental and calculated flexural capacity values.

 $V_{ACI}$  = flexural capacity calculated by Equation of ACI 318-02 (2002)

 $V_{\text{HSC}}$  = flexural capacity calculated by Equation of Ozbakkaloglu and Saatcioglu (2004)

The experimental shear strength values of both the first and second peak were evaluated with respect to the case where  $P-\Delta$  effect was not taken into consideration as well as the case where  $P-\Delta$  effect was not taken into consideration. According to Table 4.1, the experimental shear strength values of both the first and second peak of  $F_c$  80 MPa specimens are higher than the calculated values determined by Eqns. (i) and (ii) even in the case where  $P-\Delta$  effect is not taken into consideration. Because the calculated shear strength values determined by Eqns. (i) and (ii) were based on the assumption that  $\varepsilon_u$  is 0.003 equally, the shear strength from the first peak, or spalling of the cover concrete, seems to have been included. Table 4.1 also indicates that the calculated values of the specimens 'C80D22' and 'C80D19' are almost equal to the experimental values of shear strength during the first peak. The experimental shear strength values rose thereafter, too. This means that the second peak, or the shear strength under the maximum load, has a safety factor that is about 1.2 times the values calculated from Eqns. (i) and (ii), even in the case where  $P-\Delta$  effect is not taken into consideration and that the equations can be employed in the structural design.

Regarding the  $F_c$  120 MPa specimens, the experimental shear strength values during the first and second peak, on the basis of the values calculated by Eqn. (i) of Building Code and Commentary ACI 318-02 (2002), cannot be evaluated to be on the safe side. In Eqn. (ii) proposed by Ozbakkaloglu and Saatcioglu (2004), the coefficients  $\alpha_1$  and  $\beta_1$  of the Eqn. (i) are modified so that the equation can be applied to concrete columns of strengths from normal to high-strength. Using this Eqn. (ii), the experimental shear strength values during the first and second peak of  $F_c$  120 MPa specimens can be evaluated to be nearly on the safe side. However, the safety factor of the experimental shear strength values for  $F_c$  120 MPa specimens during the second peak is comparatively low with respect to that of  $F_c$  80 MPa specimens.



It is assumed that the ultimate compressive strain at extreme fiber ( $\varepsilon_u$ ) is 0.003 in the flexural capacity calculation method using these rectangular stress blocks. This is the reason why it is not suitable for calculating the shear strength during the second peak (flexural capacity) where the high-strength longitudinal reinforcements of a column undergo compressive yield phenomenon as observed in this study.

#### **5. CONCLUSIONS**

A bending shear force test was conducted on RC and PCa columns with ultra-high-strength materials subjected to varying axial load, and the following findings were obtained:

1. With almost equal calculated flexural strength provided for specimens with longitudinal reinforcements D22(# 7) (SD490) and D19(# 6) (USD685), the former developed spalling of cover concrete immediately after the compressive yield of longitudinal reinforcements, while the latter first developed spalling of cover concrete and then compressive yield of longitudinal reinforcements.

2. Specimens with a concrete design nominal strength of  $F_c$  80 MPa and  $F_c$  120 MPa were subjected to a load of compressive axial force of  $0.55F_cbD$  and  $0.50F_cbD$  respectively. The axial strains during large story drift angle in the  $F_c$ 120 MPa specimen was larger than that in the  $F_c$  80 MPa specimen, while spalling of cover concrete developed widely in the  $F_c$ 120 MPa specimen.

3. PCa column specimens of both  $F_c$  80 MPa and  $F_c$  120 MPa indicated larger shear strength during cover concrete spalling than RC column specimens. On the contrary, an increase in shear strength thereafter was small. The maximum shear strength of PCa column specimens was also a little lower than that of the RC column specimens prepared by monolithic casting.

4. The flexural capacity of each specimen was evaluated by the rectangular stress block method in compliance with Building Code and Commentary ACI 318-02 (2002). The flexural capacity levels obtained with  $F_c$  80 MPa specimens were largely on the safe side, whereas those obtained with  $F_c$  120 MPa were not necessarily on the safe side. However, it was confirmed that the experimental values were considered to be on the safe side by applying the stress blocks in accordance with the proposal of Ozbakkaloglu and Saatcioglu (2004) to the evaluation.

### NOTATION

 $A_c$  = area of core concrete within perimeter hoop (center-to-cente),  $A_g$  = gross area of column cross-section,

 $A_{st}$  = total area of longitudinal reinforcement,

b = width of a column cross-section, D = overall depth of a column cross-section

 $F_c$  = design nominal strength of concrete,  $f'_c$  = concrete cylinder compressive strength,

 $f_y$  = yield strength of longitudinal reinforcement,

P = axial load,  $P_0 =$  nominal concentric compressive capacity of a column calculated according to Eqn. 3.1,

 $P_{0(\text{HSC})}$  = nominal concentric compressive capacity of a column using concrete of strength from normal to high strength level (120 MPa) calculated according to Eqn. 3.2,

 $\alpha_1$  = coefficient that defines width of rectangular stress block,  $\beta_1$  = coefficient that defines height of rectangular stress block,  $\varepsilon_u$  = extreme copression fiber strain in concrete at ultimate moment resistance,

 $\gamma$  = coefficient defined in Eqn. 3.4

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